

## MATH

ACCELERATED EDUCATION PROGRAMME

# MATHEMATICS 

## SYLLABUS

REVISED LOWER SECONDARY (Level 1 and 2)


# ACCELERATED EDUCATION PROGRAMME MATHEMATICS 

## SYLLABUS

REVISED LOWER SECONDARY (Level 1 and 2)


MINISTRY OF

NATIONAL CURRICULUM DEVELOPMENT CENTRE

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## Revised Edition

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## Foreword

Education is a fundamental tool for the protection of conflict- and disasteraffected children and youth from harm and exploitation. This is a crucial part of UNESCO's advocacy messages. Under appropriate conditions of security, the provision of education can help protect children and youth from recruitment into fighting forces, forced labour, prostitution, drug abuse and other criminal activities. In post-conflict settings, education contributes to the reintegration into society of former soldiers and other children and youth associated with fighting forces.

Uganda's Education Act of 2008, in Part IX, Miscellaneous Provisions 49, clearly states that "there shall be non-formal education centres" for purposes of providing non-formal education. Examples of non-formal education programmes include Accelerated Education Programmes (AEPs) for the conflict areas at both primary and secondary levels, Alternative Basic Education for Karamoja (ABEK), Basic Education for Urban Poverty Areas (BEUPA), Complementary Opportunity for Primary Education (COPE) and Child-Centred Alternative Non-Formal Community Based Education (CHANCE), among others.

The National Curriculum Development Centre (NCDC), in collaboration with War Child Canada, embraced the Accelerated Education Programme (AEP) and has condensed the lower secondary curriculum to come up with the Lower Secondary Accelerated Education Programme appropriate to learners in refugee camps and the host communities of secondary school age (ages 16-45+).

The AEP at lower secondary school level focuses on completing learning in a shorter period of time, i.e., two years. The AEP is complementary both in providing an alternative route and in matching its curriculum to the 'official' curriculum, thus allowing learners to return to formal schooling at an opportune stage. The programme intends to promote access to education in an accelerated timeframe for disadvantaged groups, out-of-school and over-age children, and youth who missed out or had their education interrupted owing to poverty, violence, conflict or any calamity.

The goal of this programme is to provide learners with competencies equivalent to those in the formal system in an accelerated time frame, with learners either transitioning back into the mainstream education or exiting with some of the competencies required for work.

It is my hope that AEP will register considerable success in meeting the educational needs of these underserved populations not only in terms of access and equity, but also in helping them return to school and complete the education cycle, and especially in getting measurable learning outcomes.

I recommend the AEP and trust that the materials will be valuable in your endeavour to meet the educational needs of the refugee learners and other beneficiaries from the host communities.

## Prof. George Openjuru

CHAIRPERSON
NCDC Governing Council

## Acknowledgement

National Curriculum Development Centre (NCDC) would like to express its gratitude to all those who, in one way or another, contributed and worked tirelessly towards the development of this Accelerated Education Programme (AEP)syllabus.
Special thanks go to War Child Canada - Uganda for the financial support, their guidance in overseeing and taking timely decisions whenever necessary during the development and production of this AEP Mathematics Syllabus.

We also express our gratitude to NCDC Subject Specialists and panel members for their professional guidance and technical assistance.

Furthermore, NCDC recognises the work of the editors who worked with the writers through the development of this document.

NCDC takes responsibility for any shortcomings that might be identified in this syllabus and welcomes suggestions for addressing the inadequacies. Such comments and suggestions may be communicated to NCDC through: P.O. Box 7002, Kampala or e-mail; admin@ncdc.og.ug or website at; www.ncdc.og.ug


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## Introduction

The UNESCO Education Strategy (2014-2021) advocates for a humanistic and holistic vision of education as a fundamental human right that is essential to personal and socio-economic development. UNESCO further recommends societies that are just, inclusive, peaceful and sustainable by 2030. Vision 2040 of Uganda aims to transform Uganda into a modern and prosperous country, while the National Development Plan III (NDPIII) recognises the existing weaknesses in education, including the low efficiency and variable quality at the Secondary level. Furthermore, NDPIII focuses on enhancement of human capital, development, strengthening mechanisms for quality, effective and efficient service delivery as well as improvement of quality and relevance of skills development.

The Sustainable Development Goal 4 advocates for inclusive and quality education. The NRM Manifesto (2016-2021), emphasises continuous assessment examination systems, strengthening soft skills, which promote self-esteem, conscientiousness and a generally positive attitude to work, promoting e-learning and computer literacy in order to enhance learning outcomes.

The above aspects are lacking and where they exist, it is at a minimum level in implementation of the curriculum.
In alignment with the above policies, the Education and Sports Sector Strategic Plan (2017/20) advocates for delivery of equitable, relevant and quality education for all. The current Secondary school curriculum for Uganda, although highly regarded, has focused on the needs of a small academically oriented elite leaving out the needs of the majority of learners. The Ministry of Education and Sports (MoES) through the National Curriculum Development Centre (NCDC) therefore, undertook a review of the Lower Secondary Curriculum, aimed at providing a learning environment, opportunities, interactions, tasks and instructions that foster deep learning by putting the learner at the centre of the learning experience. This is in line with the following aims of secondary education in Uganda:

The aims of Secondary education in Uganda are to:

- Instil and promote national unity, an understanding of the social and civic responsibilities, strong love and care for others and respect for public property, as well as an appreciation of international relations and beneficial international co-operation;
- Promote an appreciation and understanding of the cultural heritage of Uganda including its languages;
- Impart and promote a sense of self discipline, ethical and spiritual values, personal and collective responsibility and initiative;
- Enable individuals to acquire and develop knowledge and an understanding of emerging needs of society and the economy;
- Provide up-date and comprehensive knowledge in theoretical and practical aspects of innovative production, modern management methods in the field of commerce and industry and their application in the context of socio-economic development of Uganda;
- Enable individuals to develop basic scientific, technological, technical, agricultural and commercial skills required for self-employment;
- Enable individuals to develop personal skills of problem solving, information gathering and interpretation, independent reading and writing, self-improvement through learning and development of social, physical and leadership skills such as are obtained through games, sports, societies and clubs;
- Lay the foundation for further education;
- Enable the individual to apply acquired skills in solving problems of community, and to develop a strong sense of constructive and beneficial belonging to that community;
- Instil positive attitudes towards productive work and strong respect for the dignity of labour and those who engage in productive labour activities;
- Develop a positive attitude towards learning as a lifelong process.


## Introduction to Accelerated Education Programme

Worldwide, substantial alternative schooling programmes are developed to meet the basic education needs of under-reached children. Of recent, it has been increasingly recognized that the goals of Education for All cannot be achieved unless more attention is paid to educating out-of-school children (UNESCO, Global Monitoring Report, 2008). Indeed, the UNESCO Global Monitoring Report 2010 'Reaching the Marginalized’ focused on this issue. In a bid to help developing countries achieve the Millennium Development Goals, there should be initiatives to incorporate elements of accelerated learning to achieve SDG 4.

The Accelerated Education Programme (AEP) in Uganda is a form of curriculum option which combines the stronger features of earlier mainstreaming approaches into the new design to raise the success rates for refugee community learners. The AEP secondary school tier is a bigger stride to address the education gap within refugee communities not only in Uganda but also other neighbouring countries. Benchmarking the Primary AEP programmes, the Secondary Education Programme intends to infer the entire process of education and its cognitive, emotional, and social components.

The Accelerated Learning Programme at Secondary school level focuses on completing learning in a shorter period of time, of two years. The AEP is complementary both in providing an alternative route and in matching its curriculum to the 'official' curriculum, thus allowing learners to return to formal schooling at some stage. The programme intends to promote access to education in an accelerated timeframe for disadvantaged groups, out of school and over-age children, and youths who missed out or had their education interrupted due to poverty, violence, conflict, and crisis. The goal of this programme is to provide learners with competencies equivalent to those in the formal system in an accelerated timeframe, with learners either transitioning back into the mainstream education or exiting with some competencies required for work.

Ideally, teaching AEP calls for a methodology that is interactive and learnercentred, incorporating other aspects of multiple-intelligence learning.

Because teaching and learning are accelerated, and the curriculum content is compressed and condensed, the four ' $P$ ' elements are at the core of the accelerated learning cycle; processes, psychological, physiological, and physical. These core elements provide the physical and psychological space in which the learner can learn more effectively.

It is intentional to include alternative subjects in this programme e.g. life skills, peace education, environment, HIV and AIDS which are responsive to the context. Learners of AEP need alternative supporting knowledge and life skills to survive in the challenging world. It is equally important to note that this conception of accelerated learning requires an extremely well-resourced classroom and exceptionally well-trained teachers. The expanded learning time from the norm is because the teaching methodology is interactive and learner centred.

It is our hope that AEP will register considerable success in meeting the educational needs of these underserved populations, not only in terms of access and equity but also in being able to return to school and completion, and most importantly in getting measurable learning outcomes.

## Background to Accelerated Education Programme

The review of AEP Curriculum was based on the situation within refugee camp in Adjumani. This hosts refugees from South Sudan where some of them had spent some time out of school. And others have never been in school.

The AEP curriculum came into existence as a catch-up programme The programme was based on the Uganda lower secondary curriculum whose cycle is four (4) years.

The Curriculum for the cycle of 4 years was compressed into two levels. Each level with a duration one (1) year.

The compression was possible because some content was removed and the other condensed.

AEP adopts accelerated learning techniques to support learners to achieve the Uganda Certificate of Education.

## The Curriculum

This curriculum focuses on four "Key Learning Outcomes" of: self - assured individuals; responsible and patriotic citizens; lifelong learners; positive contributors to society.

The curriculum emphasises knowledge, application and behavioural change. It is based on a clear set of values which must be imparted to learners during the learning process.

At the heart of every subject there are generic skills that allow development into life-long learners. Besides, there are also cross cutting issues that are embedded across subjects to enable learners understand the connections between the subjects and complexities of life

## Key Changes

The key change in the new curriculum is a move from a knowledge-based curriculum to a competency and skill- based curriculum. It is no longer sufficient to accumulate large amounts of knowledge. Young people need to develop the ability to apply their learning with confidence in a range of situations. They need to be able to use knowledge creatively. A level of competence is the ability to use knowledge rather than just to acquire it. This requires an active, learner-centred rather than passive, teacher-centred approach.
This approach to teaching and learning is in support of the Sustainable Development Goals (SDG's), otherwise known as the Global Goals. These are a universal call to action to end poverty, protect the planet and ensure that all people enjoy peace and prosperity. The key changes in the curriculum will ensure that Uganda is making good progress towards SDG 4 in particular which aims to ensure inclusive and equitable quality education and promote lifelong learning opportunities for all.

The change can be summarised in the following diagrams.

## The previous Knowledge-based Curriculum



Knowledge-based teaching was based on transferring knowledge from the teacher to the students. The teacher had knowledge and transferred this knowledge to the students by lecturing, talking, asking them to read the text book or writing notes on the board for the students to copy and learn. Students acquired the knowledge, often without fully understanding it, and were tested at the end of a unit, term or school course to see if they had remembered it. The knowledge was based mainly on the knowledge in the subjects traditionally taught at University, and little attempt was made to make it relevant to young people's own lives. The whole education system was seen by many people as a preparation for university, but the vast majority of learners do not reach university. The new curriculum will cater for this majority as well as those who later go on to University

The New Competency-based curriculum

## ACTIVITY



In the new competency-based approach, the "student" becomes a "learner". The new Learning Outcomes can only be achieved through active engagement in the learning process rather than simply absorbing knowledge given by the teacher.

The teacher needs to build on the learners' own knowledge and experience and create Learning Activities through which learners can explore the meaning of what is being learned and understand how it is applied in practical situations.

Teaching and learning becomes a two-way process of dialogue between the teacher and learners. Learners also learn from each other through discussion. Assessment also becomes a two-way process of formative and summative assessment; not just to give grades but to find out problems the learners may be having and help to solve them.

## Key Learning Outcomes

This curriculum clearly sets out 'Key Learning Outcomes' that sum up the expectations of the curriculum as a whole, and the qualities that young people will develop.
By the end of the educational process, young people will become:

## 1) Self-assured individuals who:

a) Demonstrate self- motivation, self-management and self-esteem.
b) Know their own preferences, strengths and limitations.
c) Adjust their behaviour and language appropriately to different social situations.
d) Relate well to a range of personality types.
2) Responsible and patriotic citizens who:
a) Cherish the values promoted in the curriculum.
b) Promote equity, the development of indigenous cultures and languages and appreciate other people's cultures.
c) Apply environmental and health awareness when making decisions for themselves and their community.
d) Are positive in their own identity as individuals and global citizens.
e) Are motivated to contribute to the well-being of themselves, their community and the nation.
3) Lifelong learners who:
a) Can plan, reflect and direct their own learning
b) Actively seek lifelong learning opportunities for personal and professional development
4) Positive contributors to society who:
a) Have acquired and can apply the Generic Skills
b) Demonstrate knowledge and understanding of the emerging needs of society and the economy
c) Understand how to design, make and critically evaluate products and processes to address needs.
Appreciate the physical, biological and technological world and make informed decisions about sustainable development and its impact on people and the environment.

## Values

This curriculum is based on a clear set of values. These values underpin the whole curriculum and the work of schools. They are also the values on which learners need to base their lives as citizens of Uganda. The values are derived from The Uganda National Ethics and Values Policy of 2013.

They are:

1) Respect for humanity and environment
2) Honesty; uphold and defend the truth at all times
3) Justice and fairness in dealing with others
4) Hard work for self-reliance
5) Integrity; moral uprightness and sound character
6) Creativity and innovativeness
7) Social Responsibility
8) Social Harmony
9) National Unity
10) National Consciousness and patriotism

These values are not taught directly in lessons, nor will they be assessed, but they will inform and shape all teaching and learning.

## Generic Skills

The generic skills also known by several other names, including key skills, core skills, essential skills, key competencies, necessary skills, transferable skills and employability skills are versatile skills that have wide applicability across various jobs, education, and life situations, contributing to personal and professional success and societal well-being.
Changes in the modern workplace brought about by technology, management innovations, and increased competition in the global marketplace, have led to many concerns about the adequacy of workforce skills. In response to calls to reform education to better prepare young people for the future workforce, changes to the curriculum have emphasised the teaching of general skills (e.g. problem solving, creativity, critical thinking, communication, collaboration). For this reason, generic skills lie at the heart of every subject. Apart from enabling learners to access and deepen learning across the curriculum, generic skills allow young people to develop into lifelong learners who can adapt to change and cope with the challenges of life in the 21st Century.

## MATHEMATICS SYLLABUS

Young people need to be able to think critically and solve problems at school, work and home. They need to be creative and innovative in their approach to learning and life. They must be able to communicate well in all forms, co-operate with others and also work independently. They must also be able to use functional mathematics and ICT effectively.

## 01 Critical thinking and problem-solving skills

a) Plan and carry out investigations
b) Sort and analyse information
c) Identify problems and ways forward
d) Predict outcomes and make reasonable decisions
e) Evaluate different solutions

## 02 Creativity and innovation

a) Use the imagination to explore possibilities
b) Work with others to generate ideas
c) Suggest and develop new solutions
d) Try out innovative alternatives
e) Look for patterns and make generalisations

03 Co-operation and self-directed learning
a) Work effectively in diverse teams
b) Interact effectively with others
c) Take responsibility for own learning
d) Work independently with persistence
e) Manage goals and time

## 04 Communication

a) Listen attentively and with comprehension
b) Talk confidently and explain opinions/ideas clearly
c) Read accurately and fluently
d) Write and present ideas coherently
e) Use a range of media to communicate ideas

## 05 Mathematical computation and ICT proficiency

a) Use numbers and measurements accurately
b) Interpret and interrogate mathematical data
c) Use mathematics to justify and support decisions
d) Use technology to create, manipulate and process information
e) Use technology to collaborate, communicate and refine one's work

## Generic Skills within Mathematics

These skills are not separate subjects in themselves; they are developed within the subjects of the curriculum. They also facilitate learning within those subjects. It is when these generic skills are deployed that learning is most effective.

The generic skills are a key part of the new curriculum. They have been built into the syllabuses for each of the subjects, and these subjects provide the context for the skill development. Mathematics provides a rich context for learners to communicate, co-operate, and to think critically about how the world works and to understand the world from a scientific point of view.
The Subjects also provide the contexts for progression within the skills. The same skill definitions apply to both levels, and skills progression is provided by the increasing complexity of the subject matter within each Subject. For example, within 'critical thinking', learners begin thinking critically about the relatively simple subject matter in Level 1 and then progress to thinking about the much more complex matters in Level 2.
Thus the progression is in the increasing complexity of the matters being thought about.

CRITICAL THINKING AND PROBLEM SOLVING
CREATIVITY \& INNOVATION

|  |  |  | COMMUNICATION |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \frac{\pi}{1} \\ & \frac{\pi}{\Sigma} \end{aligned}$ |  |  |  |  |  | 苍 |
|  | CO-OPERATION AND SELF-dIRECTED LEARNING |  |  |  |  |  |  |
| MATHEMATICAL COMPUTATIONS ANDICT PROFIIIENCY |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |

## Cross-cutting Issues

There are some issues that young people need to learn about, but which are not confined to one Subject. These are the 'cross- cutting Issues' and they need to be studied across the subjects. These issues develop learners' understanding of the connections between the subjects, and so of the complexities of life.

## The Cross-cutting Issues identified in the curriculum are:

1) Environmental awareness
2) Health awareness
3) Life skills
4) Mixed abilities and involvement
5) Socio-economic challenges
6) Citizenship and patriotism

These have been built into the syllabuses of each subject. The way in which they operate within the subject is very similar to the generic skills.
Mathematics provides a very good context for considering environmental and health awareness, and to understand the complex and diverse world in which we live.

## ICT Integration

Under ICT integration, ICT shall be embedded as a learning/teaching tool across all subjects. ICT teachers should endeavour to assist other subject teachers in making the ICT integration process a reality. In other subject syllabuses, ICT integration guidelines have been included.

ICT integration draft framework is summarised below:

| Category of a Task in the Syllabus | ICT Application (How ICT Will be Integrated for the Task Category) |
| :---: | :---: |
| 1) Field works | Use of cameras to take photos and record videos |
| 2) Presentations in class | Use presentation application |
| 3) Key words and meanings | Use online dictionary or search online |
| 4) Drawing/graphics | Use publishing software, Word processor |
| 5) Role play, narrations | Use audio and video recordings |
| 6) Demonstrations | Use audio and video recordings and simulations |
| 7) Locating and putting marks on an area | Use digital/online mapping |
| 8) Present findings in graphic and written format | Use desktop publishing software or word processor |
| 9) Showing data charts | Use spreadsheet software |
| 10) Group discussions | Mind-mapping software |
| 11) Search for extra reading materials | Download files on internet or by sharing |
| 12) Writing equations and formulas | Use equation editors |
| 13) Carrying out academic research | Using the Internet and other academic applications like "Encarta", "Britannica" etc. |
| 14) Sharing or learning with people across the world | Forming learning networks, formation of blogs, social media, emails etc |

## Integration of Special Needs Education (SNE)

In education system, learners of different abilities study together in the same class and in some developed countries, they are taught separately. In whatever case, the following methods are important when handling the SNE learners.

| Category of impairments | SNE Teaching Methods |
| :--- | :--- |
| Blind learners: | - Through touching |
| Learners who cannot see totally | - Use of brails |
|  | - |

## The Mathematics Syllabus

Mathematics is a compulsory subject for Level 1 and 2

## Time allocation

| Mathematics | LEVEL 1 | LEVEL 2 |
| :--- | :--- | :--- |
|  | 3 Hours per Week | 3 Hours per Week |

## Rationale

Mathematics forms a key element of every learner's education. The Mathematics programme of study emphasizes the essential mathematical skills that all citizens need for full and effective participation in civil, social and economic life. The programme of study focuses primarily on the needs of the majority of learners, some of whom may cease formal schooling before the end of Senior Four. It will allow these learners to take a wide range of formal or informal workplace opportunities, or to proceed to other postSenior Four programmes.
Prior to the reform, Mathematics throughout the Lower Secondary years was strongly geared towards the needs of the small minority of learners who might eventually go on to study Mathematics at Advanced level and beyond.
The Mathematics programme in the reformed curriculum is much more inclusive. It is designed to ensure that the majority of learners will leave school with a worthwhile, relevant qualification in the Mathematics that they will actually use in everyday life and work. In their daily life, knowingly or unknowingly, every human being uses and applies mathematical concepts in a wide range of contexts. Numeracy skills are essential to every aspect of both work and daily life. Mathematics has evolved across all cultures over the years, and it is still developing. The study of Mathematics develops the learners' reasoning and logical thinking skills, and its applications cut across all Learning Areas. During the learning process, the beauty of Mathematics and its value in a wide range of contexts are recognised by the learner.
The Lower Secondary Mathematics programme of study focuses on developing mathematical understanding, logical reasoning, problem solving and analytical thought.
The concepts, understandings and skills acquired will help learners to solve familiar and unfamiliar problems, giving them the flexibility, they need to meet new situations as they arise.

The learners will be confident with the mathematics that they use in their day-today activities in the home, in the work place, in the community, and in society.
They will also be ready to participate in civil life, using their mathematical skills to make informed decisions based on a sound understanding of facts, figures and opinions.
The skills and understanding that the learners acquire will be helpful throughout their lives. They will provide the essential mathematical tools required for a wide range of career paths including many of those in the fields of engineering, science or technology.

## Teaching and Learning: Mathematics

The thrust of the AEP syllabus is experiential and towards deeper understanding. The focus in Mathematics is on the development of understanding through mathematical enquiry and rational thought.
The AEP syllabus provides learners with a wide range of contexts in which to develop this understanding, and these contexts are designed to engage the interest of the learner and to provide opportunities to build life-related knowledge, experience and skills. Teachers are encouraged to go beyond the textbooks and provide as many meaningful contexts as possible. The generic skills have been integrated throughout the curriculum and can only be acquired through active approaches.
The role of the teacher is to build on learners' existing knowledge and experience, but to extend that by posing problems to the learners. This makes them think about their own ideas and experiences as well as adding new knowledge and skills to it.

Learners need to interact with real situations inside and outside the classroom. They need to look at pictures or diagrams, examine statistics, or read texts from a range of sources. They need to find out knowledge and ideas for themselves. They should then be expected to express these in their own words, not those of the teacher, and so demonstrate that they have understood what they have learnt.
In this approach, learners are encouraged to:

1) Be responsible for their own learning
2) Think for themselves and form their own ideas and opinions
3) Become critical thinkers, ready to face new challenges and situations for themselves
Mathematics is divided into four themes that run throughout the two levels of study. The following are the themes: Numbers, Geometry and Measures, Data and probability and patterns and Algebra.

## Topics

There are 32 topics for the two levels. They constitute 17 topics for Level 1 and 15 topics for Level 2 as shown in the Programme Planner.

Note: Content for Level 1 (year 1) is mostly drawn from Senior 1 and Senior 2, then Level 2 is Senior 3 and 4 of the Lower Secondary curriculum.

## Programme Planner

| Level 1 | Theme | Topic |  | Duration (hours) |
| :---: | :---: | :---: | :---: | :---: |
| TERM 1 | Numbers |  | Number Bases | 6 |
|  | Numbers |  | Working with Integers | 8 |
|  | Numbers |  | Fractions, Percentages and Decimals | 8 |
|  | Numbers |  | Rectangular Cartesian Coordinates in 2Dimensions | 8 |
|  | Geometry and Measures |  | Geometric Construction Skills | 6 |
| TERM 2 | Pattern and Algebra |  | Patterns and Sequences | 4 |
|  | Geometry and Measures |  | Bearing | 4 |
|  | Geometry and Measures |  | General Angle Properties of Geometric Figures | 4 |
|  | Pattern and Algebra |  | Algebra | 9 |
|  | Geometry and Measures | 10) | Business Arithmetic 1 | 4 |
|  | Geometry and Measures | 11) | Time and Time Tables | 5 |
|  | Pattern and Algebra | 12) | Mapping and Relations | 6 |


| Level 1 | Theme | Topic | Duration (hours) |
| :---: | :---: | :---: | :---: |
| TERM 3 | Pattern and Algebra | 13) Translation and Vector | 6 |
|  | Data and Probability | 14) Graphs | 6 |
|  | Numbers | 15) Numerical Concepts | 10 |
|  | Data and Probability | 16) Set Theory | 7 |
|  | Pattern and Algebra | 17) Equations of a Straight Line | 7 |
|  |  | Total | 108 |


| Level 2 | Term | Topic | Duration <br> (hours) |  |
| :--- | :--- | :--- | :--- | :---: |
| TERM 1 | Patterns and Algebra | 1) | Inequalities and <br> Regions | 6 |
|  | Data and Probability | 2) | Data Collection and <br> Presentation | 12 |
|  | Geometry and <br> Measures | 3) | Similarities and <br> Enlargement | 6 |
|  | Geometry and <br> Measures | 4) | Reflection and <br> Rotation | 6 |
| TERM 2 | Data and Probability | 5) | Ratios and <br> Proportions | 6 |
|  | Data and Probability | 6) | Matrices | 6 |
|  | Measures and | 7) | Matrix <br> Transformations | 8 |
|  | Patterns and Algebra | 8) | Simultaneous <br> Equations | 4 |


| Level 2 | Term | Topic | Duration ( hours) |
| :---: | :---: | :---: | :---: |
|  | Patterns and Algebra | 9) Quadratic Equations | 8 |
|  | Geometry and Measures | 10) Trigonometry | 10 |
| TERM 3 | Geometry and Measures | 11) Circle | 8 |
|  | Geometry and Measures | 12) Nets, Areas and Volumes of Solids (Mensuration) | 7 |
|  | Geometry and Measures | 13) Business Mathematics 2 | 6 |
|  | Data and Probability | 14) Probability | 7 |
|  | Geometry and Measures | 15) Lines and Plane in Three Dimensional Geometrical Figures | 8 |
|  |  | Total | 108 |

## References

Use the teaching and learning materials as recommended by the ministry of education and sports Uganda

Level 1: Senior 1 and Senior 2 materials
Level 2: Senior 3 and Senior 4 materials

## DETAILED SYLLABUS

## LEVEL 1

## TERM 1

## Topic 1: Number Bases

Duration: 6 Hours

## Overview

In this topic, the learner will learn how to compute and appreciate the meaning of number bases and converting numbers in other bases other than base ten (decimal). You will learn the relationships amongst the various bases.

Competency: The learner uses decimal place value to develop understanding of numbers written in other bases.

| Learning Outcomes | Suggested Teaching \& Learning Ac | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) Identify number $s$ in any base using abacus. (k) | 1) Identify situations in which you have ever used number bases in real life situation. <br> 2) Playing number games, for example matching numbers in base two with numbers in base ten e.g., 1111 base two is matched to 15 base ten <br> 3) Write numerical values of different bases (e.g.) base two uses 0,1 <br> 4) Make an abacus using local available materials to: <br> a) identify place values in different bases <br> b) state value of a digit | 1) Observe <br> learners in their groups trying to identify place values of various number bases using abacus and converting numbers from one base to |

Learning Outcomes

Suggested Teaching \& Learning Activities
2) Convert number $s$ from one base to another. (u)
3) Manipul ate number $s \quad$ in different bases with respect to all the four operatio ns. (u s)
4) Identify place value in different bases.
(u)
c) manipulate numbers in different bases with respect to all four operations (addition, subtraction, multiplication and division)
5) Use a digit stop watch to demonstrate conversion of seconds to minutes. Imagine living in cartoon world where people have just eight digits rather than ten. What would their arithmetic be like?
6) Design counters in different number bases using strips threaded through card:
7) Prepare strips numbered 0 to 7 , thread through a card so that a single number on each strip is displayed, use to make different numbers. Change the length of the strips to investigate different number bases (e.g., 2222 in base 8). Hint:

> a) Convert numbers 1 to 15 from base ten to base two

## Sample

Assessment
Strategies
another.
2) Observe individual learners in their groups whether they are cooperative, whether they collaborate with their colleagues.
3) Let
individual learners explain how they have identified the place values and converted numbers from one base to another e.g. How do you find $p$ and $q$.

If $10020_{\text {base } p}=$

| Learning <br> Outcomes | Suggested Teaching \& Learning Activities | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
|  | b) Place the numbers in four boxes provided according to the conversion above <br> c) When a number appears in the box, record it as 1 and when it does not appear, then record it as 0 . <br> E.g., Guess number7. 7 does not appear in the first box but appears in other 3 boxes... so $7_{\text {ten }}=0111_{\text {two }}$ <br> The number of boxes depends on the largest number in base ten that one chooses to use. | $87_{\text {base }}$ ? <br> 4) Complete the addition/mu Itiplication table for different number bases. |

## Hints to the Teacher

1) Carry out diagnostic assessment of the learners on number bases.
2) For any base beyond base twelve the numerals used must be defined.
3) For better understanding of place values of various bases, use abacus (involve learners in making their own abaci).
4) Let learners identify where number bases are used in real life situation.

## Topic 2: Working with Integers

## Duration: 8 Hours

## Overview

In this topic, there is extension of numbers from millions to trillions. The learners should learn how to read and write numbers in words correctly and also learn different types of numbers and relationships amongst them.
Competency: The learner carries out calculations with positive and negative integers.

## Learning Outcomes

The learner should be able to:

1) Identify, read and write natural numbers as numerals and words in million, billion and trillion (u, s).
2) Differentiate between natural numbers and whole numbers/ integers. (u)
3)Identify even, odd, prime and composite numbers. (u)
3) Identify factors and multiples of numbers.
4) Work out divisibility tests of some numbers, (u s)

## Suggested Teaching \& Sample Assessment <br> Learning Activities

1) Write natural numbers of choice in words and vice versa.
2) Order numbers and locate them on a number line.
3) Use directed number in context e.g., temperature, height above and below sea level, floors in a building.
4) Investigate multiples on a 1-100 square and notice that the digital root (i.e., the sum of the digits) of multiples of three is always a multiple of three, and for multiples of nine the digital root is a multiple of nine.
5) Observe learners as they discuss in groups how they can read and write natural numbers in words and differentiate between natural and whole numbers.
6) Observe the interaction of learners within their groups.
7) Nambi has four number cards: She can arrange the cards to form different numbers. For example, she can form the number 3407

Learning Outcomes
6) Relate common factors with h.c.f and multiples with l.c.m. (u)
7) Identify directed numbers. (k)
8) Carry mathematical operations on numbers using the rules of integers. (k)
9) Use bodmas rule to carry out the four mathematical operations integers. (u)
10) Use directed numbers (limited to integers) in real life situations. (u, s)

## Suggested Teaching \& Sample Assessment <br> Learning Activities <br> Strategies

Determine how to distinguish other multiples (e.g., 2 (even numbers), 5,10 ).
5) Investigate the factors of numbers 1 to 30 .
6) Which numbers have just two factors? Which numbers have an odd number of factors?
7) Use exactly four $4 s$ to make as many whole number answers between 1 and 100 e.g. $(4+4 \times 4) \div 4=(4+16) \div$ $4=5$, recording the calculations correctly.
8) Determine the prime factorisation of any integer.

\section*{| 3 | 4 | 0 | 7 |
| :--- | :--- | :--- | :--- |}

What is the greatest even number Nambi can form using all four of her number cards? What is the least odd number she can form using all four of her number cards?
4) How many hundreds are there in one million?
5) What are the prime factorisations of 942 and 357 ? Hence find the HCF of 942 and 357, and the LCM.

## Hints to the Teacher

1) Attention must be taken in writing numbers given in figures and vice versa (commas must be used while writing in figures and avoid the use of the word (and) when writing in words.
2) For better understanding of concepts by learners, introduce different concepts one at time.
3) When dealing with mixed operations, the order of operations should be followed.
4) Let learners identify where integers are applied in real life.

## Topic 3: Fractions, Percentages and Decimals

Duration: 8 Hours

## Overview

This topic looks at numbers which are not whole but just parts of whole numbers. These parts can be fractions or decimals. There are relationships between whole numbers, fractions and decimals.
Competency: The learner understands and uses fractions, decimals and percentages.

|  | Suggested <br> \& Learning A | Sample |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) describe different types of fractions. (k) | 1) Draw a circle on a piece of paper and cut it out. <br> 2) Fold the cut out and shade off | 1) Let the learners explain to the group members how Moses would carry out the activity below. |
| 2) | different types of fractions including decimals. <br> 3) Understand | 2) Observe the learners as they give the explanation. Look out for, whether the |
| 3) add, subtract, divide and multiplies | as with ten as a tor |  |
| 4) apply solve situati | hundredths, etc.). <br> 4) Understand | can contribute to the explanation. <br> 3) Moses has the |
| 5) add, subtract, divide and multiply decimals. ( $u, s$ ) | fractions with 100 as <br> the denominator. | 3) Moses has following cards. $\begin{array}{llll} 3 & 4 & 0 & 7 \end{array}$ |
| 6) convert fractions to decimals and vice versa. (u, s) | 5) Play <br> games <br> matching <br> fractions, percentage and decimals. | What is the least number Moses can form using all five of his cards? |

## Learning Outcomes

7) identify
and classify decimals into terminating, non -terminating and recurring decimals. (u)
8) convert recurring decimals into fractions ( $u, s$ ).
9) convert fractions and decimals into percentages and vice versa. (u,s)
10) calculate a percentage in of a given quantity. (s)
11) work out real life situations
involving
percentages. ( $u, s$, v/a)

Suggested Teaching Sample \& Learning Activities Strategies
6) Identify percentages in every day contexts.
7) Use a calculator to investigate fraction- decimal equivalence which fractions produce terminating decimals and which fractions produce recurring decimals?
8) Develop strategies for converting decimals to fractions.
9) Solve problems that involve fractions, percentages and decimals.
4) How many 0.01 s are there in:

- 1
- 0.1
- 10
- 30

Rose achieved a score of 21 out of 25 in a mathematics test, and a score of 31out of 40 in a physics test. Did she do better in mathematics or in physics? Justify your answer.

## Hint to the Teacher

1) Guide the learners to understand the meaning of a fractions.
2) Guide the learners to identify different types of fractions.
3) Guide the learner to relate percentages and decimals to fractions and vice versa.
4) Let learners identify where fractions, decimals and percentages are applied in real life.

## Topic 4: Rectangular Cartesian Coordinates in 2 Dimensions

 Duration: 8 Hours
## Overview

In this topic, the learner shall understand how to locate the position of a point, object, and place from a given starting point which may be called a point of origin.

Competency: The learner plots and interprets points in a range of contexts.

| Learning Outcomes | Suggested <br> Teaching and <br> Learning Activities | Sample Assess |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) draw and label the Cartesian plane. (k,s) <br> 2) identify the $x$ and y - axis. (k) <br> 3) read and plot points on the Cartesian plane. <br> 4) complete shapes on a coordinate grid. ( $\mathrm{k}, \mathrm{u}, \mathrm{s}$ ) <br> 5) choose and use appropriate scale for a bivariate data set. (u, s, v/a) | 1) Create <br> rectangular <br> cartesian plane using a piece of paper. <br> 2) Draw shapes on a coordinate grid given the coordinates of one or more. <br> 3) Collect data (e.g., height and head circumference) from your class and plot a scatter graph. | 1) Observe learners as they try to do the activities below. Look out for their cooperation in the process of getting solutions for the given questions below, sharing of information. <br> 2) The heights and ages of five girls have been plotted on the scatter graph. <br> a) Who is the tallest and how tall is she? <br> b) Who is the same age in years as Dembe? <br> c) How much taller is Faith than Joan? |

## Learning Suggested <br> Outcomes Teaching and <br> Learning Activities <br> Sample Assessment Strategies

3) Two vertices of a square are at the points $(2,1)$ and $(6,3)$. What are the coordinates of the other two vertices of the square? There are three possible answers. Find all three Vertices

## Hint to the Teacher

1. Guide the learners to understand the position of negative and positive numbers on the axes (Cartesian plane).
2. Emphasis should be put on choosing suitable scales.
3. Let learners identify where rectangular cartesian coordinates in 2 dimensions are applied in real life.

## Topic 5: General Angle Properties of Geometric Figures

Duration: 4 Hours

## Overview

In this topic the learner will draw, form and identify different angles. The learner will be able to understand how to use angle properties of polygons to solve problems in real situations. This is a hands-on topic, so the learner is encouraged to be practical.
Competency: The learner uses the angle properties of lines and shapes to solve problems.

| Learning Outcomes | Suggested Teaching and Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) identify different angles. (k) <br> 2) solve problems involving angles at a point on a straight line, angles on a transversal and parallel lines. (k, u, s) | 1) Draw various angles and identify acute, obtuse and reflex angles. <br> 2) Draw and label a pair of parallel lines and a line crossing them (transversal) Identify alternate, corresponding and supplementary angles on the diagram drawn above. <br> 3) Add another transversal to determine the angle sum of a triangle. <br> 4) Cut out three identical isosceles triangles from a scrap card. Arrange them to form a trapezium PQST. | 1) Observe the learners as they carry out the following tasks: <br> Expected diagrams <br> 2) Through what angle do you turn in each of these cases? <br> a) You are facing North and you turn: clockwise to face SE <br> b) anti-clockwise face SE <br> c) You are facing NW and you turn to face SE |


| Learning Outcomes | Suggested Teaching and Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| 3) know and use the angle sum of a triangle. (k, u) <br> a. state and use angle propertie $s$ of polygons when solving problems . (u, s) | 5) $R$ is the midpoint of the line QS. $P Q=P R=T R=T S .$ <br> Note: the drawing is not accurate. <br> a) Explain why $P Q=P R$. <br> b) Find two more lines that are equal to PQ and PR . <br> c) Find the values of the labelled angles a, b, c, d, e, f, g <br> 6) Find the angle sum of polygons by considering the minimum number of triangles within a polygon. Hence find the interior and exterior angles of regular polygons. | 3) How many sides does each regular polygon have, if the exterior angle is 720 ; 240; 60o; 450; 400? <br> 4) Three interior angles of a pentagon are 1100,1000 , and 1200 respectively. The fourth and the fifth angles are $3 \times 0$ and $2 \times 0$. Find their values. <br> 5) Observe their collaboration, respect for one another and attitude towards the task. |

## Hint to the Teacher

1) Encourage learners to acquire and use mathematical sets.
2) The schools should provide chalk and mathematical chalkboard instruments for demonstration.
3) Let learners identify where General angle properties of geometric figures are applied in real life.

## Topic 6: Patterns and Sequence

Duration: 4 Hours

## Overview

In this topic, the learn gets to understand how to determine the happening of the event based on the knowledge of the previous event. In this particular topic, the sequences and patterns are the numbers.

Competency: The learners explore number patterns and sequences.
$\left.\begin{array}{|l|l|l|l|}\hline \begin{array}{l}\text { Learning } \\ \text { Outcomes }\end{array} & \begin{array}{c}\text { Suggested Teaching and Learning } \\ \text { Activities }\end{array} & \begin{array}{l}\text { Sample } \\ \text { Assessment }\end{array} \\ \text { Strategies }\end{array}\right]$

| Learning <br> Outcomes | Suggested Teaching and Learning Activities | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
| a <br> sequence . (k, s) <br> 4) describe <br> a general rule <br> when a pattern is given. (k, $\mathrm{u}, \mathrm{s})$ <br> 5) determin <br> e terms in sequence . (u, s) | 4) Put the numbers $1,2,3,4,5 \ldots$ into this number machine to generate a sequence. <br> - Write down the first five members of the sequence. <br> - What is the formula for the nth term in the sequence? <br> 5) Sharon wants to shade some multiples on a 1 to 100 square to make a pattern of horizontal lines. Can she do this? Explain your answer. <br> 6) Draw a double machine that could be used to generate the sequence 5,8 , 11, 14, 17.... | 2) Observe the following; collaboratio n , harmony amongst the members of the groups, willingness to do the activity. <br> Write a formula for the $\mathrm{n}^{\text {th }}$ term in a sequence starting: <br> i) $1,1,1$, $1, \ldots$ <br> ii) $1,4,9$, 16, 25, |

## Hints to the Teacher

1) Emphasis should also be put on number patterns.
2) Guide learners to develop number patterns.
3) Relate patterns to sequences.
4) Let learners identify where Patterns and Sequences are applied in real life.

## Topic 7: Bearings

Duration: 4 Hours

## Overview

The learner will not find challenges in this topic if he/she is well-grounded in the previous topics on Geometry which include; General Angle Properties of Geometric Figures. The learner will understand and describe the bearing of a point from a given point.

Competency: The learner uses compass points, bearings and scale drawings.

| Le | Suggested Teaching and Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) know the compass points. <br> (k) <br> 2) describe the direction of a place from a given point using compass points. (u s) <br> 3) describe the bearing of a place from a given point. (ks) <br> 4) apply bearings in real life situations. (u s) | 1) Match compass points with bearings. <br> 2) Create a scale drawing of the classroom or school. <br> 3) Alex is facing North. He turns clockwise to face West. What angle has he turned through? <br> 4) Henry's school is 4 km away from his home, on a bearing of $070^{\circ}$. The market is 1 km away from the school on a bearing of $250^{\circ}$. The hospital is 6 km away from the market, on a bearing | 1) Let the learners in groups, discuss and explain how they will accomplish the following task: <br> 2) Two Ships leave Port Bell at the same time. One ship sails 80 km on a bearing of 0300 to position A. The other ship sails 160km on a bearing of 1100 to position B. <br> 3) Use a scale drawing to find: a) the distance AB |


| Learning Outcomes | Suggested Teaching and Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| 5) choose and uses an appropriate scale to make an accurate drawing. (ku) <br> 6) differentiate between sketch and a scale drawing. (u, v) | of $310^{\circ}$. <br> What is the bearing of the hospital from Henry's home? <br> a) Make a scale drawing to find the distance and bearing of the hospital from Henry's home. <br> b) Remember to state the scale you use on your drawing, and give your answer to a sensible degree of accuracy. | 4) b) the bearing of $B$ from $A$ <br> 5) During the process of accomplishing the task, observe the communication skills of individual learners, creativity, respect for one another, sharing of information amongst themselves and other values and skills. |

## Hint to the Teacher

1) Emphasise the difference between sketching and accurate drawing.
2) Emphasise practical work in bearings.
3) Let learners identify where are applied in real life.

## Topic 8: Geometric Construction Skills

Duration: 6 Hours

## Overview

Choosing suitable scales, measuring and drawing is prerequisite knowledge for this topic. The learner should be able to develop construction skills The topic is hands on.

Competency: The learner uses the angle properties of lines and shapes to solve problems.

| Le | Suggested Le Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) Draw perpendicular and parallel lines. (k, s) <br> 2) Construct parallel lines, perpendicular lines, angle bisectors and mediators. (u,s) <br> 3) Ruse a pair of compasses and a ruler to construct special angles. $\left(90^{\circ}\right.$, $60^{\circ}, 45^{\circ}$ ) (u, s) <br> 4) Describe a locus. (u) <br> 5) Relate parallel lines, perpendicular bisector, angle bisector, straight line and a circle as a | 1) Learners should identify perpendicular and parallel lines in the environment <br> 2) Outside learners use strings and markers to create various loci e.g., equidistant from a fixed point (circle); equidistant from two fixed points (perpendicular bisector); equidistant from a line (parallel lines); equidistant from a fixed point and a line (parabola); the sum of the distance | 1) Observe learners as they select correct instruments to use. Observe their interaction, attitude towards what they are supposed to do. Do they differentiate drawing from constructing? <br> 2) Let the learners explain or describe the procedure of constructing angles. |



## Hint to the Teacher

1) Emphasize the difference between construction and drawing of angles and other shapes.
2) Emphasize the difference between sketching and accurate drawing in construction.
3) Emphasize practical work in construction.
4) Let learners identify where Geometric construction skills are applied in real life.

## Topic 9: Algebra

Duration: 9 Hours

## Overview

In this topic, the learner will understand how to manipulate mathematical expressions involving unknowns.

Competency: The learner forms and uses simple algebraic expressions.

| Learning <br> Outcomes | Suggested Learning Activities | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) use letters to represent numbers. (u) <br> 2) write statements in algebraic form. <br> (u) <br> 3) simplify algebraic expressions (to include algebraic fractions). (u, s) <br> 4) evaluate algebraic expressions by substituting numerical values. (u, s) | 1) Write an expression for each statement .use the variables to represent unknow numbers <br> 2) Use number machines and write the equivalent algebraic expressions e.g. <br> when x is put into this machine the output is $3 x-2$ <br> 3) Thirty books are bought for sh. 10 800. Some cost UGX 400 each and the others UGX 300 each. How many books of each value are bought? | 1) As they discuss, observe participati on in each group, presentati ons, methods used. <br> 2) Find the missing input and output numbers in these double number machines: |

## Learning Outcomes

5) manipulate simple algebraic equations in one variable and solve them. (u, s, $\mathrm{v} / \mathrm{a}$ )
6) recognise equivalent quadratic expressions. (k u s)
7) expand algebraic expressions. (k s)
8) identify perfect squares.
(u)
9) factorise quadratic expressions. (u s)
10) solve quadratic equations where the quadratic expression can be factorised. (k s)

## Suggested Learning Activities

4) In groups, draw a triangle and label as shown.

5) The perimeter of the triangle above is 26 cm . Determine the lengths of the triangle.
6) The sum of two numbers is 10 and their product is 21 . What are the numbers?
7) What is the connection with $2 x(10-x)=21$ and $x-10 x+21=0$ and $(x-3)(x-7)=0$ ?
8) Investigate the relationship between multiplication and finding the area of a rectangle, and generalise to algebra


## Sample

Assessment

## Strategies

3) Solve the following equations:
a) $3 p-2=8$
b) $2 x+1=3 x-$ 2
4) Yusuf thinks of a number,
b. He adds
6. He multiplies the sum by 4. He subtracts twice the original number. His result is 32.
a) Construct an
equation to
represent Yusuf's work.
b) Solve the equation

| Learning <br> Outcomes | Suggested Learning Activities | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
|  | 9) Multiply pairs of linear expressions $(x+a)$ to generate quadratic expressions recognising the special cases of perfect squares $(x+a)^{2}$ and the difference of two squares $x^{2}-a^{2}=(x+a)(x-a)$ <br> 10) Substitute values of $x$ in quadratic expressions and note the values when the expression is zero - link with the solutions of the quadratic equation. <br> 11) Investigate when quadratic expressions can be factorised to establish $x^{2}+(p+q) x+p q=(x+p)(x+q)$ | to find Yusuf's original number. |

## Hints to the Teacher

1) Use real life situations in order not to make algebra abstract.
2) Guide the learners to understand the difference between linear and nonlinear expressions.
3) Let learners identify where Algebra is applied in real life.

## Topic 10: Business Arithmetic 1

Duration: 4 Hours

## Overview

The learner should understand the day today mathematics being used at home. This topic should draw experience from the learner's environment. Let it be practical.

Competency: The learner understands and applies Business arithmetic.

| Learning Outcomes | Suggested <br> Teaching <br>  <br> Learning <br> Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) describe and calculate profit, loss (includes all expenses incurred), commission, interest and discount. (u, s) | 1) In groups, let the learners discuss the cost of producing certain goods like pancakes, chapatis etc. and determine the selling price of the products. <br> 2) They should | 1) Observe learners whether they are doing the work as instructed (integrity), are they willing to do the work? positive attitude towards work). How is their presentation of the work? <br> 2) Are they creative and innovative? <br> 3) In a school there are 100 |
| 2) express profit or loss <br> as percentage. | use it to demonstrate how to make profit, loss and | students, each of whom is given 3 litres of milk per week. <br> 4) If a half-litre pack costs |
| 3) solve simple interest problems. (k ,s, v/a) | their percentages for the goods produced. | UGX 1500, find the monthly milk bill (use 1 month $=4$ weeks) |


| Learning Outcomes | Suggested <br> Teaching <br> Learning <br> Activities | Sample Assessment <br> Strategies |
| :---: | :---: | :---: |
| 4) calculate <br> compound <br> interest using step by step method to a maximum of 3 years. | 3) Describe how you can calculate, commission, interest, insurance and discount. | 5) A trader marked the prices of his goods $20 \%$ above the cost price and allowed a discount of $10 \%$ to the customers on the marked price. If Okot paid sh. 54 000 for a shirt, what was the marked price of the shirt? What was its cost price? |

## Hint to the Teacher

1) The formula for compound interest should not be introduced at this level 1.
2) Let learners identify where Business arithmetic 1 is applied in real life.

## Topic 11: Time and Time Tables

Duration: 5 Hours

## Overview

Time management is a skill and therefore, this topic will help the learner develop this skill by drawing her/his personal timetable. Competency: The learner understands and uses time.

| Learning <br> Outcomes |  <br> Learning Activities | Sample Assessment Activities |
| :--- | :--- | :--- | :--- | :--- |


| Learning <br> Outcomes |  <br> Learning Activities | Sample Assessment Activities |
| :--- | :--- | :--- | :--- |

## Hint to the Teacher

1) This topic should be taught practically.
2) Emphasis should be put on duration of time when changing from AM to PM and vice versa.
3) Let learners identify where time and time tables are applied in real life.

## Topic 12: Relations, Mapping, and Functions

Duration: 6 Hours

## Overview

In this topic, the learner will understand how to determine a relationship between objects and develop logical skills in this topic.
Competency: The learner understands and uses arrow diagrams/mappings to represent relations and functions.

The learner should be able to:

1) use arrow diagrams
/mappings to represent relations and functions. (k, u)
2) identify domain and range of a mapping. ( $k, u$ )
3) describe and distinguish between a function and non- function mappings. (u, s)
4) understand and use function notation. (k, u, s)

| Learning | Suggested Teaching <br> Outcomes | Sample Assessment |
| :--- | :--- | :--- |

Suggested Teaching Sample Strategies

1) Observe the learners in their groups as they complete the task below. Find out the learners' attitude towards the group work; are learners communicating effectively? Are they learning from one another? Are they creative and critical?
2) Do these mapping diagrams represent functions? Give
reasons for your answers.


## Hint to the Teacher

1) Leave out composite function and inverse function.
2) Let learners identify where relations, mappings and functions are applied in real life.

## Topic 13: Translation and Vectors

Duration: 6 Hours

## Overview

In this topic, the learner should be able to understand that translation and vectors are forms of transformations in given direction.

Competency: The learner understands the nature of vector, manipulates and represents them in order to define translation.

|  | Suggested Teaching \& Learning Activities | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> a) describe translation as a transformation. <br> (u) <br> b) differentiate between scalars and vector quantities. ( $k, u$ ) <br> c) use vector notation. (k, s) <br> d) represent vectors both single and combined geometrically. (u, s) <br> e) apply vectors in real life situations. (us) | 1) lets learners move objects to the left, right, up and down in class or outside. task them to explain their observations at each stage. <br> 2) Describe the translation of the purple polygon in the diagram below. <br> 3) Distinguish (magnitude only) and vectors (magnitude and direction), | In groups, let the learners discuss the following task: <br> 1) What is the vector that translates T to U? <br> 2) What is the vector that translates $U$ to T? <br> 3) Observe them as they discuss the task. |

## Learning <br> Outcomes

f) describe position vector
geometrically and as a column vector. (k, u)
g) find out the vector of a directed line segment and its magnitude when position vectors of the end points are known. (u)
h) find out the position vector of the mid-point of the line segment. (u)

|  |  |
| :--- | ---: | :--- |
| Learning Activities | Sample <br> Assessment <br> Strategies |

4) Investigate moving objects plotted on a coordinate grid without changing their orientation - use a vector a to define the translation where a represents movement parallel to the $x$ axis and $b$ represents movement parallel to the $y$ axis.
5) Investigate how to 'undo' a translation; the effect of performing more than one translation - draw diagrams to illustrate findings.
6) Isabirye wants to swim directly across a river. The river flows at a speed of 1.5 metres per second. Isabirye can swim at a speed of 2.5 metres per second. Use a scale drawing to find out:
a) At what angle to the river bank should Isabirye face in order to swim directly across the river?
b) What will his velocity be?
7) Recall and review, what is the difference between a vector
8) Assess the learners on the core values and generic skills.

| Learning Outcomes | Suggested Teaching <br> Learning Activities | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
|  | and scalar quantity? Give examples. <br> 8) Identify parallel and equal vectors. <br> 9) Use vector addition and subtraction. <br> 10) Explore the use of position vectors to define positions on a coordinate grid, including the midpoint of a line segment and proportional division of a line. |  |

## Hint to the Teacher

1) Teach the topic practically.
2) Let learners identify where Translation and Vectors are applied in real life.

## Topic 14: Graphs

Duration: 6 Hours

## Overview

The learner will be able to understand that graphs are forms of displaying information for easy analysis, interpretation of information and making decisions/conclusions based on what is displayed on the graphs.
Competency: The learner plots, interprets and uses graphs to solve problems.

| Learning |
| :--- |
| Outcomes |
| The learner |
| should be able |
| to: |
| 1) tabulate |
| values from |
| given |
| relations (u). |
| 2)choose and <br> use <br> appropriate <br> scales (u). <br> 3) plot and draw | lines through given points (us).

4) draw, read and interpret the graph

| Learning Outcomes | Suggested Teaching \& Learning Activities | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
| (e.g., <br> Distance- <br> Time graph, Speed-Time graph to estimate distance, speed and time) ( $u, s$, $\mathrm{v} / \mathrm{a}$ ) | journey from Soroti to Kampala. | friend's house? <br> 3) How long did Atim stay at the house? <br> b) How long did it take Atim to walk back from her friend's house? <br> c) Draw the speed-time graph for Atim's journey. |

## Hint to the Teacher

1) Emphasis should be put on use of suitable grid paper (squared paper).
2) Guide the learners on choosing the suitable scale to use.
3) Let learners identify where Graphs are applied in real life.
4) Emphasize graphs as a form of pattern.

## Topic 15: Numerical Concepts

Duration: 10 Hours

## Overview

In this topic, the learner would be able to understand how to write numbers in various forms for easy manipulation.

Competency: The learner manipulates indices, standard form and surds.


Learning Outcomes
us)
6) use a calculator to find powers and roots. (k, u, s)
7) use surds to represent roots that cannot be represented exactly as decimals. (k, u)
8) manipulate and simplify expressions with surds. ( $u, s, v / a$ )

Suggested Teaching Learning Activities
the universe? How far is it from the Earth to the moon? To the sun?
4) Investigate numbers that can't be written exactly on a calculator e.g., thirds, sevenths, pi.
5) Investigate the difference between significant figures, decimal places.
6) Rewrite a surd in its simplest form by ensuring the number underneath the root sign has no square numbers as factors.
7) Use the importance laws of surds, which can be derived from the laws of indices to help simplify surds.

Sample Assessment Activities
225."

Who was correct? Justify your answer.
The population census of 1969 found that the population of Uganda was 9500 000.

The population census of 2011 found that
it was 32900000.
Tushabe said, "The population rose by 23400 000."

Mariam said,
"The population rose by $2.34 \times$ 107."

Who was correct?
Justify your answer.

## Hints to the Teacher

1) School should acquire standard mathematical tables.
2) Guide learners to use scientific calculators.
3) Let learners identify where Numerical concepts are applied in real life.

## Topic 16: Set Theory

Duration: 7 Hours

## Overview

The learner will be able to categorise items according to the given characters, rules or relationship.
Competency: The learner uses sets to solve real life situations.

| Learning Outcomes | Suggested Teachin Learning Activities |
| :---: | :---: |
| The learner should be able to: <br> 1) describe a set and identify elements of a set. (k, u) <br> 2) identify different types of sets and their symbols (empty set, universal set, equal set, complement , disjoint set, intersection set union set, subset). (k) | i) Familiarise themselves with set notation <br> ii) Draw and interpret diagrams to illustrate relationships between sets, apply to practical contexts |


| Learning | Suggested Teaching | \& | Sample | Assessment |
| :--- | :--- | :--- | :--- | :--- |
| Outcomes | Learning Activities |  | Strategies |  |

3) determine
the number
of elements
in a set. (u,
s)
4) represent
and show
different
operations
on sets by
shading the
different
regions in a
Venn
diagram. (k, u, s)
5) apply sets to practical
situations
using two
and three
sets. (u, s,
v/a)
not eat a meal.
i) Represent this information in set notation
ii) Represent the information on a Venn diagram.
iii) How many guests ate both meat and chicken?
iv) How many guests had meat?
6) In a school there is an Arts Club, a Science Club, and a Mathematics Club. 30 learners in one class belong to at least one of the clubs. 15 belong to the Arts Club, 12 belong to the Science Club, and 13 belong to the Mathematics Club.
What is the maximum number of learners that could belong to all three clubs?

## Hint to the Teacher

1) Guide learners to write information from word problems into set language.
2) Guide the learners to begin with two Venn diagrams and continue to three Venn diagrams.
3) Let learners identify where set theory is applied in real life.

## Topic 17: Equation of a Straight Line

Duration: 7 Hours

## Overview

In this topic, the learner will explore the relationship between points and variables. Under some conditions, the variables or points are equal.

Competency: The learner understands and uses linear equations and their graphs.

|  |  |  |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) form linear equations with given points. (k, s) <br> 2) draw the graph of a line given its equation. (u, s) <br> 3) understand the relationship between a linear equation $y=m x+c$ and its graph. (k, u) <br> 4) determine the $x$ and $y$ intercepts of a given linear graph and a | 1) Determine the equation for each set of points that form a straight line. <br> 2) Investigate the properties of the equation of a straightline $y=m x+c$, by plotting the graphs using different values of $m$ and $c$ <br> 3) How do you get parallel lines? How do you make the line steeper? <br> 4) Consider a ladder of length 10 m . <br> 5) Place the foot of the ladder at: i) 8 m , ii) 5 m , iii) 2 m from the wall and lean the ladder against the wall. <br> 6) What happens to the angle between the ground and the ladder as the foot of the | 1) Observe the learners in their groups as they carry out the tasks below. During the process, are learners communicating effectively? Are they learning from one another? Are they creative? <br> 2) Asabi is going to plot the graphs of these six equations: $\begin{aligned} & y=2 x+1, \quad y=3 x, \\ & y=x+4 \end{aligned}$ |


| Lea | Suggested Teaching \& Learning Activities | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
| given linear equation. (u s) | ve |  |
| 5) determine the gradient of a straight line. ( $u$, s) | 7) Relate the steepness of the ladder with the distance between the wall and the foot of the ladder. Explain | thout plotting e equations: ich graph will steepest? |
| 6) state the gradient of a straight line when given the equation. (k, u) | this relationship. <br> 8) Review how does the equation $\mathrm{y}=\mathrm{mx}+\mathrm{c}$ work? <br> 9) Introduce gradient as a measure of steepness/rate | Which will have the greatest $y$ intercept? Are any of the lines parallel or |
|  | of change |  |
| relationship of gradients of parallel and perpendicular | 10) Draw a straight line and a perpendicular line on a coordinate grid. What are their equations? Try for | Explain your answer. <br> 1. Sendi drew the graphs of $2 x-$ |
| lines to determine the | other pair. What do you tice about the gradients? | $3=y$ and $y=7$ on the same set of axes. |
| straight line. (k $u, s)$ | 11) Investigate the least number of points that need to be plotted to draw a straight line. | What are the coordinates of intersection? |

## Hint to the Teacher

1) Emphasis should be put on use of suitable grid paper (squared paper)
2) Learners need to be aware that $x$ is measured on the horizontal axis and y on the vertical axis
3) Let learners identify where the equation of a straight line is applied in real life.

## LEVEL 2

## Topic 1: Inequalities and Regions

Duration: 6 Hours

## Overview

In this topic, the learner will be able to differentiate equations from inequalities, manipulate inequalities, draw and show the required regions (feasible
region).
Competency: The learner presents and solves problems involving inequalities.


## Learning

 Outcomes4) represent linear inequalities graphically. (k, u, s)
5) form simple linear inequalities for regions on a graph. $(u, s)$

Suggested Teaching \& Learning Sample Assessment Activities

4) Play foxes and chickens where chickens are positioned on a coordinate grid and inequalities are used as fences to protect the chickens from foxes.

## Strategies

they learning from one another? are they creative?
3) Solve the linear inequalities and represent the solutions on a number line
$2 x+7<x+10$
$2 x+7<x+10$
4) Use inequalities to define a square region that has $(1,1)$ at its centre.

## Hint to the Teacher

1) Emphasis should be put on use of suitable grid paper (squared paper).
2) Guide learners on identification of wanted and unwanted regions.
3) Emphasis on when to use solid lines or dotted lines depending on the nature of the inequalities.
4) Let learners identify where inequalities and regions are applied in real life.

## Topic 2: Data Collection and Presentation

Duration: 12 Hours

## Overview

In this topic, the learner will develop the skills of collecting data, display it in various forms, interpret and analyse to make conclusions.
Competency: The learner collects and represents different sorts of data.

## Learning Outcomes

The learner should be able to:

1) understand the differences between the types of data. (k, u)
2) collect and represent simple data from local environment using tally chart, bar chart (bars do not touch), pie chart and line graph. (k, u, s, v/a)
3) understand mode, mean as a measure of
location/tendency and knows how to find them and when to use them. (k, u, s)
4) understand range as a measure of dispersion /spread and how to find it. ( $k, u, s$ )

Suggested Teaching \& Learning Activities

1) Class to get in height order - stand in a circle to illustrate the range (difference between tallest and shortest person).
2) Discuss representative/typic al values - find the most popular height (mode), the middle height (median), what if we were all the same height? (The mean).
3) Compare the advantages and disadvantages of mean, median and mode in different contexts.
4) Explore the need for grouping data when there are many different values. Once grouped, exact statistics (mean, median, mode,

Sample Assessment Strategies

1) Observe the learners in their groups as they carry out the task below. During the process are learners communicating effectively?
2) Are they learning from one another? Are they creative and critical?
3) Which measure of central tendency would be best as a representative value for: salaries in a company workforce, crop yields, examination grades (A, B, C, D, $E)$, measurements in a science experiment. Justify your

## Learning Outcomes

5) draw and use frequency tables for ungrouped data. (u, s)
6) draw and use frequency tables for grouped data. (u, s)
7) estimate measures of location and dispersion for grouped data. (u, s)
8) calculate the mean using an assumed mean. ( $u, s$ )
9) draw a histogram with equal class intervals and use it to estimate the mode. (u, s)
10) draw a cumulative frequency curve (ogive) and uses it to estimate the median. ( $u, \mathrm{~s}, \mathrm{v} / \mathrm{a}$ )

Suggested Teaching \& Sample Assessment Learning Activities Strategies
range) cannot be choice. determined.
i) Compare estimates from grouped data with the actual values from the raw data.
ii) Draw a histogram and estimate the mode

iii) Draw a cumulative frequency graph and estimate the median
iv) Collect data for a purpose and apply techniques to draw conclusions.
4) The cumulative frequency diagram shows the time taken by 100 people to complete 10 press-ups.

Find an estimate for the median time. Explain why only an estimate for the median is possible


## Hint to the Teacher

1) Emphasize the collection of data from the environment by learners.
2) Emphasis should be put on use of suitable grid paper (squared paper).
3) Emphasise use of appropriate scale.
4) Let learners identify where data collection and presentation is applied in real life.

## Topic 3: Similarities and Enlargement

Duration: 6 Hours

## Overview

The learner will be able to understand that similarities and enlargement are forms of transformation.

Competency: The learner understands and applies relationships between lengths, areas and volumes of similar shapes and objects.

| Learning Outcomes | Suggested Teaching \& Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) identify <br> similar <br> figures. (u, <br> s) <br> 2) state and use the properties of similar figures. (k, u) <br> 3) define enlargemen t. (k) <br> 4) state the properties of enlargemen t to construct | 1) Explore different similar shapes by matching proportion of their sides and angles (e.g.) <br> 2) The photo below shows cubes and plastic balls. Consider the photo and answer the questions that follow. <br> 3) True or false: the cubes are similar to each other. <br> 4) True or false: the plastic balls are not similar to each other. <br> 5) Explore enlarging shapes through different centres of | 1) Observe the learners in their groups as they discuss the activity below. Find out the learners' attitude towards the group work, integrity, are they doing the work in harmony? <br> 2) During the process of the description, are learners communicating effectively? Are they learning from one another? Are they creative and critical? <br> 3) Let the learners give their group reports. <br> Activity: Bayo and Sara want to find the height of a tree. They cannot climb the |

## Learning Outcomes

objects and images. (k)
5) state the relationship between linear, area and volume scale
factors. (u, s)
6) apply scale factors in real life situations. (u s) (Hint include map extracts)

Suggested Teaching \& Sample
Assessment Learning Activities Strategies tree. Instead, they measure Sara's own height, the length of Sara's shadow, and the length of the tree's shadow. The table shows their results.


What is the height of the tree?
Give your answer to a reasonable degree of accuracy.

## Hint to the Teacher

1) Teach similarity first before enlargement.
2) Teach ratios and proportions using a recipe, medicinal syrup etc. and the effects of misusing or correctly using ratios and proportions in real life.
3) Emphasis should be put on use of suitable grid paper (squared paper).
4) Guide the learners on how to choose the suitable scale to use.
5) Let learners identify where similarities and enlargement are applied in real life.

## Topic 4: Reflection and Rotation

Duration: 6 Hours

## Overview

The learner will be able to understand that reflection and rotation are forms of transformation.

Competency: The learner reflects and rotates shapes in a range of contexts.

|  | Suggested Teaching <br> Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) Identify lines and planes of symmetry for different figures. (k) <br> 2) reflect shapes and objects. (u, s) <br> 3) apply reflection in the cartesian plane. (u, s) | 1) Write down numbers $0,1,2$, $3,4,5,6,7,8,9$ on the paper. Place a mirror at each of the numbers above. <br> a) try to read the image of the numbers. <br> b) write down the images of these numbers. <br> c) comment on the image of 0 in comparison to the 'object' 0 . <br> 2) The learner should cut shapes from scrap card and trace the different shapes on plain sheet of paper. <br> a) Rotate the shapes about an identified centre of rotation through an angle. <br> b) Trace out the images and let them discuss the characteristics of the object and image being rotated at | 1) In groups, learners should carry out the task below; observe them as they do the task. Is there harmony in the groups? Is each learner's attitude towards the activity positive? How are they communicating to each other? Are they learning from each other? Look at their presentations. <br> 2) Let each group explain to the other groups how they have carried out the task. |

## Learning

 Outcomes4) describe and state the order of
rotational
symmetry of plane figures. (k, u, s)
5) identifies the
difference
between
clockwise
and anticlock wise rotation. ( $k, u$ )
6) states properties of rotation as a transforma tion include congruenc e. (k, u)

## Suggested Teaching

 Learning Activitiesdifferent centres and angles of rotation.
c) Let the learners draw the different shapes with their images
3) Identify all the lines of symmetry in the letters of the alphabet written as capital letters, repeat for numbers
4) Use a mirror to reflect objects in a given line of symmetry
5) Investigate what happens to the coordinates of the image when an object is drawn on a coordinate grid and reflected in each axis and the lines $y=x$ and $y=-x$
6) Cut out a regular polygon from card and mark one corner. Make an outline on paper.

How many different ways will the card polygon fit inside the outline of the polygon? e.g., An equilateral triangle has order of rotation 3.

Repeat for other regular polygons.

## Sample Assessment

Strategies
3) Task: Plot the points A (1, 2), B ($1,1)$ and $C(-4,3)$ on a Cartesian plane. Join up the points to create the object. After a reflection the image has points $A^{\prime}$ $(2,1), B^{\prime}(1,-1)$ and $C^{\prime}(3,-4)$

Find the equation of the line of reflection.
4) In pairs, let the learners discuss the following tasks. Observe them as they discuss. Assess the learners on the core values and generic skills.
5) Plot the points $P(-$ $2,1), \mathrm{Q}(0,2)$ and R $(1,2)$ to form the triangle PQR on a square grid.

Rotate PQR about the point ( 0,0 ) through an angle of

| Learning Outcomes | Suggested Teaching \& Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| 7) determine $s$ the centre and angle of rotation. ( $u, s$ ) <br> 8) applies properties of rotation in the Cartesian plane. (u, $\mathrm{s}, \mathrm{v} / \mathrm{a}$ ) | 7) Are there any capital letters of the alphabet that have rotational symmetry? <br> 8) Cut shapes from scrap card, draw around the shape on a plain sheet of paper to create the object. <br> 9) Rotate the card shape about an identified centre of rotation ( 0 ) through an angle, and in a given direction (clockwise or anticlockwise). Draw around the card to create the image. <br> 10) Investigate rotating different shapes on plain paper and a coordinate grid. <br> 11) Given an object and image, construct the centre of rotation. | $90^{\circ}$ clockwise. What are the coordinates of the image of triangle PQR after the rotation? <br> Determine the centre of rotation and the angle of rotation. |

## Hint to the Teacher

1) Use congruence to explain reflection and rotation
2) Emphasis should be put on use of suitable grid paper (squared paper)
3) Guide the learners on how to choose suitable scale to be used.
4) Teach reflection before rotation.
5) Guide the learners to do the work practically.
6) Let learners identify where reflection and rotation are applied in real life.

## Topic 5: Ratios and Proportions

Duration: 6 Hours

## Overview

In this topic the learner will be able to understand dividing in given ratios, sharing in the given proportions and differentiate the various proportions.
Competency: The learner understands ratio and proportion, and uses them in a range of contexts.

|  |  |  |
| :---: | :---: | :---: |
| The learner should be able to: <br> 1) underst and and apply equival ent ratios. <br> (u, s) <br> 2) underst <br> and and <br> apply <br> direct <br> and <br> inverse <br> proporti <br> onal <br> reasoni <br> ng. (u, <br> s) | 1) Use diagrams to illustrate ratios. Look at the diagrams. <br> a) Use the diagrams to fill in the gaps and complete the equivalent ratios. <br> b) Draw diagrams to show some ratios that are equivalent to 5:3 <br> c) Simon says, "12:15 is equivalent to $3: 4$ ". Is he correct? Draw diagrams to justify your answer. <br> 2) Adjust recipes e.g., 8 cakes need 400 grams of flour. How much flour for 20 cakes? How many cakes with 750 grams of flour? These are examples of | 1) Observe the learners in their groups as they carry out the tasks below. During the process, are learners communicating effectively? are they learning from one another? are they creative and critical? <br> 2) Mrs Mukasa is a smallscale poultry farmer. It costs her UGX. 250000 to buy the feed to raise 70 broilers. <br> a) Mrs Mugisha wants to raise 300 broilers. How much will the feed needed to raise these broilers cost? <br> b) Day old broiler chicks cost UGX. 2000 each. Mrs Opio has UGX. 1 |

Learning
Outcomes
3) underst and and apply ratio, proporti on and scale.
( $k, u, s)$
a) draw and interpret the line of best fit when looking for a relations hip in bivariate data on a scatter graph. ( $u, s$ )

Sample Teaching \& Learning Sample Activities
direct proportion,

## $y \propto x$

3) A rectangle has an area of 36 square units. If the dimensions of the rectangle are $x$ and $y$, what is the relationship between $x$ and $y$ ? Plot a graph to show the relationship, this is an example of inverse proportion,

## $y \propto \frac{1}{x}$

4) Collect data from the class e.g., handspan and height. Plot a scatter graph. Draw a line of best fit. Use the line of best fit to estimate the handspan of someone joining the class with a particular height.

## Strategies

000000 (one million shillings). She wants to buy and raise as many chicks as she can. How many should she buy?
3) The height and mass of horses are shown on the scatter graph. What is the equation of the line of best fit? Estimate the height of a horse of mass 600 kg.


## Hint to the Teacher

1) Help learners to distinguish between ratios and proportions.
2) Let learners identify where ratios and proportions are applied in real life.

## Topic 6: Matrices

Duration: 6 Hours

## Overview

A matrix is a rectangular arrangement of numbers or letters. The learner will be able to understand that a matrix is one way of keeping information.

Competency: Learner understands and uses matrices.


| Learning Outcomes |  <br> Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| do so. (k, u, s) <br> 5) apply <br> knowledge <br> of matrices <br> in solving <br> problems <br> from real <br> life <br> situation. <br> ( $u, s, v / a$ ) | e) Use matrices to solve pairs of linear equations in two unknowns. <br> f) Explore what happens when there are no solutions. | 3) Use the matrix method to show that the following pairs of simultaneous equations have no unique solutions. Why does this happen? <br> (a) $\begin{aligned} & 6 x-9 y=36 \\ & 2 x-3 y=5 \end{aligned}$ <br> (b) $\begin{aligned} & 3 x-7 y=45 \\ & 9 x-21 y=135 \end{aligned}$ |

## Hint to the Teacher

1) Guide the learners to identify and understand columns and rows in class.
2) Guide the learners to appreciate special matrices.
3) Let learners identify where matrices are applied in real life.

## Topic 7: Matrix Transformations

Duration: 8 Hours

## Overview

The learner will be able to understand that matrix transformation is a form of transformation in which the matrices are used.
Competency: The learner understands and uses matrices to transform shapes on a coordinate grid.

| Learning Outcomes | Suggested Teaching <br> Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> a) derive transformation matrices for reflection, rotation and enlargement. (k, $\mathrm{u}, \mathrm{s}$ ) | i) Find the matrix corresponding to the transformation by considering the images of the point $I(1,0), J(0,1)$ and $K(1,1)$ : <br> a) reflection in the line $x$ $+y=0$ | 1) Observe the learners as they carry out the tasks below. During the process, are learners communicating effectively? Are they learning from one another? Are |
| b) determine the image given the object and transformation matrix, on a coordinate grid. ( $u$, s) | b) a 90degrees anticlockwise rotation about the origin <br> c) an enlargement, centre the origin, scale factor k. What do you notice about | they creative and critical? <br> $\mathrm{O}(0,0), \mathrm{A}(3,0), \mathrm{B}(3$, $3)$ and $C(0,3)$ are the vertices of a square $O A B C . A^{\prime}(4,2), B^{\prime}(6,6)$ and $C^{\prime}(2,4)$ are the |
| c) determine the matrix of transformation when the object and its image are given. ( $u$, $s$ ) | the determinant of the transformation matrix? <br> ii) Plot the following five triangles on grid paper. | vertices of $O A^{\prime} B^{\prime} C^{\prime}$, the image of OABC such that the origin is invariant. |
| d) determine the a matrix that transforms the image back to | $\begin{aligned} & \mathrm{T}_{1}(1,1),(5,1),(5,3), \\ & \mathrm{T}_{2}(1,1),(1,5),(-1,5) \\ & \mathrm{T}_{3}(-1,1),(-5,1),(-5,3) \end{aligned}$ | (a)the transformation matrix <br> (b) the area of $O A^{\prime} B^{\prime} C^{\prime}$. |

## Learning Outcomes

the object. ( $u, s$ ))
e) use the inverse matrix to find the object when the image is given. ( $u, s$ )
f) Investigate the relationship between area scale factor and determinant of the
transformation matrix. (u)
g) determine a single matrix for successive transformations. ( $u, v / a$ )

Suggested Teaching \&
Learning Activities
$\mathrm{T}_{4}(-1,-1),(-5,-1),(-5,-3)$ and
$\mathrm{T}_{5}(1,-3),(1,-5),(5,-3)$
iii) Describe a single transformation that maps:
a) $T_{3}$ onto $T_{1}$.
b) $\mathrm{T}_{4}$ onto $\mathrm{T}_{5}$
c) T 1 onto T 2
d) T 4 onto T 3
e) T 1 onto T 4
f) $T_{4}$ onto $T_{2}$, and determine the transformation matrix.
iv) Determine the transformation matrix to 'undo' each transformation. What do you notice?
v) Investigate combining transformations and the corresponding transformation matrices.

## Sample Assessment Strategies

2) Describe the transformations defined by the matrices and Evaluate $A B$ and BA.
3) Describe the transformation each represents. A shape $P$ is subject to transformation $A B$ to give image $P_{A B}$. The same shape $P$ is subject to transformation $B A$ to give image $\mathrm{P}_{\text {ва }}$.
4) Describe the single transformation that will map $\mathrm{P}_{\mathrm{AB}}$ to Рва. $^{\text {. }}$

## Hint to the Teacher

1) Guide the learners to discover some of the transformation matrices using a unit square.
2) Guide learners to always use transformation matrix as a pre- multiplier.
3) Emphasise that the matrix that transforms an image back to an object is the inverse of the matrix that transforms an object to an image.
4) Let learners identify where matrices of transformations are applied in real life.

## Topic 8: Simultaneous Equations

Duration: 4 Hours

## Overview

Simultaneous equations are equations which involve more than one variable or unknown that can be solved at the same time to give values which satisfy each of them.

Competency: Learners should understand, form, solve and use simultaneous equations in real life situation.


## Learning

 Outcomes4) use matrices to solve
simultaneous
equations. (u, s, v/a)

## Suggested Teaching \& Learning Activities <br> iii) Explore <br> different methods for

 solving simultaneous equations including substitution, elimination and use of matrices.iv) Represent simultaneous equations graphically. From Senior 3, Topic 1 , plot $2 x-3=y$ and $y$ $=7$ on the same set of axes. What are the coordinates of intersection? What do the values represent?

## Sample

Assessment

## Strategies

3) Use substitution to solve the simultaneous equations:

$$
3 x+y=-2
$$

$$
4 x+2 y=0
$$

4) Draw graphs for the following pairs of simultaneous equations, which have no unique solutions. Why does this happen?
a) $6 x-9 y=36$

$$
2 x-3 y=5
$$

b) $3 x-7 y=45$
$9 x-21 y=135$
c) $x+y=3$
$2 y=6-2 x$

## Hint to the Teacher

1) Guide the learner to handle one method at a time (don't mix up methods).
2) Emphasis should be put on use of suitable grid paper (squared paper).
3) Guide the learners on how to choose the suitable scale to be used.
4) Let learners identify where simultaneous equations are applied in real life.

## Topic 9: Quadratic Equations

## Duration: 8 Hours

## Overview

In this topic, the learner will differentiate between linear and quadratic equations. A quadratic equation is a second order polynomial equation in one variable.
Competency: Learner understands, solves and use quadratic equations in real life situation.

|  | Suggested Teaching Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> a) determine <br> the roots of quadratic equations using factorisation, completing the square and the formula. (k, u, s) <br> b) b) form a quadratic equation given its roots. (u, s) | i) Create a table of values for the quadratic equations: $y=x^{2}, y=x^{2}-4, y=(x+1)^{2}$. <br> ii) Describe the transformations that link these graphs. Find the solutions to the equation <br> iii) $x^{2}=0, x^{2}=4,(x+1)^{2}=0$ How do the solutions relate to the graph? <br> - A school has a rectangular garden with an area of 1000 m 2 . Its length is 30 m greater than its width. Find the dimensions of the garden. <br> - Explore completing the square to solve quadratic equations and relate to graphs | 1) Observe the learners in their groups as they work on the tasks below. During the process, are learners communicating effectively? Are they learning from one another? Are they creative and critical? <br> 2) A room $p$ metres long and (p-3) metres wide, has an area of $40 \mathrm{~m}^{2}$. Obtain an equation in $p$. <br> Find the value of $p$. <br> 3) The roots of $a$ quadratic equation are -2 and 3 , write down at least three different equations |

\section*{Learning Outcomes

c) c) make a • Generalise completing table of values for a quadratic function and draws the graph. (k, u, s)
d) link the solutions of a quadratic equation with its graphical representatio n. (k, u, s)
e) solve
simultaneous equations involving one quadratic equation and a linear equation. (u s)

\section*{Suggested Teaching

## Suggested Teaching Learning Activities

 Learning Activities} the square to derivation of the quadratic formula for$$
\begin{aligned}
& a x^{2}+b x+c=0 \\
& x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
\end{aligned}
$$

- Investigate when quadratic equations have two distinct, a single (repeated) and no real solutions and match to the graphs.

iv) Solve equations involving a quadratic equation and a linear equation, and represent graphically.


## Hint to the Teacher

1. Emphasis should be put on use of suitable grid paper (squared paper)
2. Guide the learners on how to choose the suitable scale to be used.
3. Guide the learners to form linear equations from quadratic.
4. Let learners identify where quadratic equations are applied in real life.

## Topic 10: Trigonometry

Duration: Hours

## Overview

The learner should be able to understand that trigonometry is the only geometry that deals with three sided figures.
Competency: The learner understands, justifies and applies the three basic trigonometry functions.

| Learning Outcomes | Suggested Teaching \& Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| The learner should be able to: a) derive sine, cosine and tangent functions from the unit circle. (kus) | i) Draw a circle radius 1 unit $(10 \mathrm{~cm})$ on graph paper and add axes as shown - the centre of the circle should be on an intersection of major grid lines. For different values of angle $\theta$ measure $x$ | 1) Observe the learners in their groups as they carry out the tasks below. During the process, are learners communicating effectively? Are they learning from one another? Are they creative and critical? |
| b) read and use calculators to find values of trigonometric functions. (u s) <br> c) use sine, cosine and tangent in calculating lengths of sides and angles of right-angled triangles. find angles of elevation and depression. (k s) | the table. <br> On separate graphs, plot graphs of $x$ and $y$ against $\theta^{\circ}$ <br> Compute $y \div x$, plot $y \div x$ against $\theta^{\circ}$ <br> include trigonometric functions. <br> ii) Review, particularly the graphs of trigonometric | 3) Find the height above the ground of a hot air balloon, whose angle elevation from the ground 1 km away. <br> 4) In pairs, let the learners discuss the following tasks. Observe them as they discuss. Assess the learners on the core values and generic skills. |

Learning
Outcomes
d) determine
trigonometric
ratios of angles
greater than
900. (urr s)
e) use the graphs of trigonometric functions to determine values of sine, cosine and tangent for any angle. (us)
f) apply sine and cosine rules to solve real life problems. (k u s)
iii) Use the graph to explain how values of the trigonometric functions outside the interval $\left[-90^{\circ}, 90^{\circ}\right]$ are related to values in that interval. Solve trigonometric equations over different intervals.
iv) Apply the sine and cosine rules.

functions and their Solve
relationship with the unit circle


## Suggested Teaching Sample <br> Assessment \& Learning Activities Strategies

$$
\begin{gathered}
\sin \theta=0.5, \quad 0^{\circ} \leq \theta \leq 720^{\circ} \\
\cos \theta=\frac{\sqrt{2}}{2},-360^{\circ} \leq \theta \leq 360^{\circ} \\
\tan \theta=-1,-180^{\circ} \leq \theta \leq 540^{\circ}
\end{gathered}
$$

The hour and minute hands of a clock have lengths of 44 mm and 57 mm respectively.
a) Calculate the distance between the ends of the hands when the angle between the hands is $69^{\circ}$.
b) Calculate the angle between the hands when the ends of the hands are 32 mm apart
5) A pole 8.3 metres long and a pole 11.5 metres long are placed on the ground with two ends in contact with each other.
6) The distance between the other two ends is 4.7 metres. Find the angle between the two poles at the point of contact.

## Hint to the Teacher

1. Guide the learners to identify the signs of the trigonometrical ratios using the unit circle.
2. This topic should be taught practically.
3. Let learners identify where trigonometry is applied in real life.

## Topic 11: Circle

Duration: 8 Hours

## Overview

Learners should be able to understand, justify and apply the formulae for the area and circumference of a circle. They should also be able to understand and use circle properties to solve problems.

Competency: The learner understands, justifies and applies the formulae for the area, circumference and uses circle properties to solve problems.
$\left.\begin{array}{l|l|l|l}\text { Learning } \\ \text { Outcomes }\end{array} \quad \begin{array}{l}\text { Suggested Teaching \& Learning } \\ \text { Activities }\end{array} \begin{array}{l}\text { Sample } \\ \text { Assessment } \\ \text { Strategies }\end{array}\right\}$

| Learning Outcomes | Suggested Teaching \& Learning Activities | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
| e) identify arc, chord, sector and segment. (k) | iii) How can you fit a circular cake on a rectangular plate? What are the least dimensions of the plate? | 2) During the process of the presentation |
| f) draw the tangent to the circle. (k) |  | , are learners communicat ing |
| g) relate and compute |  | ey |
| an arc at the Centre and | iv) Apply the formulae for circumference and area enclosed by a circle in everyday contexts. | other? are ey creative d critical? |
|  |  | $t$ the arners |
| h) determine the angle properties of the circle. (u) | $\pi r^{2}$ to find arc lengths and areas of sectors and segments. (Note use trigonometry to derive area of a triangle is $1 / 2 a b \sin C$ ) | eir |
| i) determine and use the properties of a cyclic quadrilateral. ( $u, s$ ) | v) Cut a right-angled triangle from a piece of paper. In another piece of paper make a slit so one corner of the triangle can fit through snugly. Move the corner around, maintaining the snug fit and trace the locus of the | 3) The Wheels of a Bicycle have a diameter of 70 cm . |
| j) determine the length of the common | corner. What do you notice? <br> Repeat for the other corners. | distance travelled by the |


| Learning <br> Outcomes | Suggested Teaching \& Learning Activities | Sample <br> Assessment <br> Strategies |
| :---: | :---: | :---: |
| chord for two intersecting circles. (u, s) <br> k) calculate the area of sectors and segments. (u, $\mathrm{s}, \mathrm{v} / \mathrm{a}$ ) | vi) Find the centre of the circle. <br> For a given chord measure the angle at the centre and the angle at the circumference of the major segment. What do you notice? Prove it. Repeat for the minor segment. <br> vii) Use the results above to derive and prove the properties of cyclic quadrilaterals. <br> viii) Investigate the properties of tangents to a circle. <br> ix) Find the length of the common chord when two circles intersect. | Bicycle when the Wheels turn through $300^{\circ}$ <br> 4) (a) Given that $\mathrm{Acm}^{2}$ is the area of a circle of a diameter $d$ cm, show that $A=\pi \mathrm{d}^{2} / 4$ <br> (b) Use the formula in (a) to find the diameter of a circle of area $25 \mathrm{~cm}^{2}$ |

## Hint to the Teacher

1) Encourage learners to acquire and use mathematical sets.
2) Guide learners to discover the circle properties practically.
3) Let learners identify where circles are applied in real life.

## Topic 12: Nets, Areas and Volumes of Solids (Mensuration)

Duration: 7 Hours

## Overview

The learner will be able to understand the nets of various solids and this will enable him/her to determine the surface areas and volumes of various solids.

Competency: The learner should be able to make and draw 2D and 3D shapes, and explore their properties.

|  | Suggested Teaching Learning Activities | Sample |
| :---: | :---: | :---: |
| The learner should be able to: <br> a) identify common solids and their properties including faces, edges and vertices. (k) <br> b) form nets of common solids. (u s) <br> c) state units of measures. (k) | i) Provide learners with cardboard, packages and count the faces, edges and vertices. Dismantle to find the net. <br> ii) •How many different nets of the following solids can they create? <br> - Cube <br> - Cuboids <br> - Square based pyramid | 1) Observe the learners in their groups as they carry out the task below. <br> During the process, are learners communicating effectively? <br> Are they learning from one another? Are they creative and critical? <br> Task: A tent has a cuboid base and a pyramidal roof. <br> a) Sketch a net of the tent, and indicate the lengths of its edges. <br> b) Calculate the surface area of the tent. <br> c) Sketch as many different nets as you |


| Learning Outcomes | Suggested Teaching \& Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| d) convert units from one form to another. (u) <br> e) calculate <br> surface <br> areas of <br> three- <br> dimensiona <br> I figures. (u, <br> s) <br> f) calculate the volume of cubes and cuboids. (u, s) | iii) Put learners in groups to make these three shapes out of strips of wood that are all the same length. <br> How many strips are needed for each shape? <br> iv) How many different cuboids can be made from 24-unit cubes? | can for the tent. <br> Note: Learners may discuss whether the floor of the tent is covered. Such an observation would indicate that they are thinking mathematically. |

## Hint to the Teacher

1) Encourage learners to make nets of different 3-D shapes using locally available materials.
2) Let learners identify where mensuration is applied in real life.

## Topic 13: Business Arithmetic 2

## Duration: 6 Hours

## Overview

The learner will understand the day-today usage of business mathematics in daily life. This topic should draw experience from the learner's environment. Like market places.

Competency: The learner understands and applies business mathematics when solving problems.

| Learning Outcomes | Suggested <br> Teaching <br>  <br> Learning <br> Activities | Sample Assessment <br> Strategies |
| :---: | :---: | :---: |
| The learner should be able to: <br> a) Use <br> multiplier <br> when <br> calculating <br> percentage <br> change. (u, s) | i) Let the learners set up imaginary shops in the classroom. <br> ii) Let the learners set the cost and | 1) Observe the learners in their groups as they carry out the tasks below. During the process, are learners communicating effectively? are they learning from one another? are they creative and critical? |
| b) calculate compound interest using the formula. (u, s) | selling prices. <br> Learners can calculate the profit for each item sold. | 2) A piece of sculpture and painting together cost UGX 21 000. The painting costs twice as much as the piece of sculpture. Find the cost of the |
| c) understand and calculate depreciation and appreciation. $(\mathrm{u}, \mathrm{s})$ | iii) When shopping which is the best saving: two for the price of one, | painting. <br> 3) The marked price of a set of curtains is UGX 75000 , but there is a cash discount of UGX 12.50 on every sh100. Find the cash price for the |

Learning Outcomes

Suggested
Teaching

## Learning <br> Activities

d) understand and convert local or foreign currencies. (u, s)
e) understand and calculate hire purchase.
(u)
f) describe and determine
Mortgage of assets. (us)
g) calculate income tax given income tax bands. (u, v/a)
one third off, pay 20\% tax and then have a discount of $50 \%$, have a discount of $50 \%$ and then pay $20 \%$ tax?
iv) A shop has a sale, $25 \%$ off all prices. I buy a pair of shoes for sh. 60000. What was the price of the shoes before the sale?

## Sample Assessment

Strategies
curtains.
4) If a forex bureau buys Kenyan shilling at the rate of UGX 42 per Kenya shilling, find:
5) The amount in Uganda shillings paid out by the Bureau in exchange for K shillings 625.
6) The amount in Kenya shillings that can be exchanged for Uganda shillings 5460.
7) Ashok invests UGX 100000 in a savings account that pays $10 \%$ compound interest each year. Assuming no further money is invested and no withdrawals are made, how many years does it take to double his money?

## Hint to the Teacher

1) Guide the learners to use step -by -step approach to derive the compound interest formula.
2) Let learners visit nearby businesses like school canteen, nearby market to get real life experiences.
3) Let learners identify where business arithmetic 2 is applied in real life.

## Topic 14: Probability

## Duration: 7 Hours

## Overview

This topic will help the learner to use the happenings of something in the past and present in predicting the happenings in future in order to bring out the relationship between the patterns and probability.

Competency: The learner applies his/her understanding of probability to predict events and solve a wide range of problems.

| Learning | Suggested Teaching \& Sample | Assessment |  |
| :--- | :--- | ---: | :--- |
| Outcomes | Learning Activities |  | Strategies |

should be able to:
understand the terms random, experiment, outcome, sample space, event and probability. (k, u)
a) construct the probability space. (u, s)
b) determine probabilities from experiments and real-life

The learner i) Discuss the likelihood of Suggested Teaching \&
Learning Activities
i) Discuss the likelihood of different events and order them from impossible to certain. Introduce the probability scale from 0 to 1.

ii) In pairs, get an unbiased coin. Mark one side of the coin as a 'head (H)' and the second side as a 'tail (T)'. Toss the coin 100 times, recording the outcome each time e.g., H, T, T, ...
iii) Plot a graph to show the proportion of heads after each throw.

1) Observe the learners as they work on the tasks below.
2) During the process, are learners communicating effectively? are they learning from one another? are they creative and critical?
3) Sara has the following coins in her pocket bag: UGX 50; UGX 100; UGX 200; UGX 500; UGX 1000. She selects a coin at random to put into a charity collection box.
4) What is the probability that she:
a) gives more than UGX 200

| Learning <br> Outcomes | Suggested Teaching <br> Learning Activities | Sample <br> Strategies |
| :--- | :--- | :--- | :--- |
| data. (u, s) |  |  |


| Learning Outcomes | Suggested Teaching \& Learning Activities | Sample Assessment Strategies |
| :---: | :---: | :---: |
| f) use Venn diagrams to determine probabilities. ( $u, s, v / a$ ) | possibility space to determine the theoretical probabilities. <br> vii) Use a tree diagram to determine the theoretical probabilities. <br> viii) Apply probability in a variety of contexts including those that can be described using a Venn diagram. | 7) In a school, there is an Arts Club, a Science Club, and a Mathematics Club. 30 learners in one class, each belongs to either one or two of the clubs. 15 belong to the Arts Club, 12 belong to the Science Club, and 13 belong to the Mathematics Club. Draw a Venn diagram. <br> What is the probability of belonging to at least two clubs? |

## Hint to the Teacher.

1) Teach probability concepts practically.
2) Let learners identify where probability is applied in real life.

## Topic 15: Lines and Plane in Three Dimensional Geometrical Figures

Duration: 8 Hours

## Overview

The learner will understand and make use of the characteristics of lines and planes in making 3-D Geometrical figures to solve societal problems

Competency: The learner understands and applies lines and planes in 3D to solve problems.

|  |  |  |
| :---: | :---: | :---: |
| The learner should be able to: <br> a) apply Pythagora s theorem in 3D to calculate the distance between two points. (u, s) <br> b) determine the angle between a | i) Collect polyhedra and for each one, record the number of faces, edges and vertices. Determine the relationship between the number of vertices, edges and faces. <br> ii)Construct a square based pyramid using four equilateral triangles and a square. Use Pythagoras' theorem to determine the perpendicular height of the pyramid, check by measuring your model. | 1) Observe the learners in their groups as they discuss how to work out the activity below. Find out the learners' attitude towards the group work, integrity, are they doing the work in harmony? <br> 2) During the process of the presentation, are learners communicating effectively? are they learning from one another? are they creative and critical? <br> 3) Let the learners hand in |


| Learning Outcomes | Suggested Teaching \& Learning Activities | Sample Assessment <br> Strategies |
| :---: | :---: | :---: |
| s) <br> c) determine the angle between two planes. (u, s) | iii) Construct a net for a square based pyramid whose perpendicular height is half the length of the square. How many of these will fill a cube? <br> iv) What is the angle between the triangular faces and the square face? What is the angle between the triangular faces? | 4) A wireless mast is held vertically by four stays 10 m long, fixed to the mast at the same height and joined to the four corners of a square on level ground. If each stay is inclined at $60^{\circ}$ to the horizontal. Calculate the height of the top of each stay and the length of a side of the square |

## Hint to the Teacher

1) Encourage learners to make nets and models of different 3-D shapes.
2) Emphasis should be put on use of right-angled triangle.
3) Let learners identify where three dimensional geometry is applied in real life.

DEVELOPMENT CENTRE

## Assessment

## Assessing the New Expectations for Learning

The AEP curriculum sets expectations for learning, with a shift from Learning Outcomes that focus mainly on knowledge to those that focus on skills and deeper understanding. These Learning Outcomes require a different approach to assessment.

The "Learning Outcomes" in the syllabus are set out in terms of Knowledge, Understanding, Skills, and Values/Attitudes. This is what is referred to by the letters k, u, s \& v/ a.

It is not possible to assess values/attitudes in the same way as knowledge, understanding and skills because they are more personal and variable and are long-term aspirations. This does not mean that values/attitudes are not important. It means that we must value things that we cannot easily assess. So, this guidance booklet focuses on knowledge, skills and understanding.

| Knowledge | The retention of information. |
| :--- | :--- |
| Understanding | Putting knowledge into a framework of meaning- |
| Skills | The ability to perform a physical or mental act or operation. |
| Values | The inherent or acquired behaviours or actions that form a c <br> haracter of an individual. |
| Attitudes | A set of emotions, beliefs or behaviours toward a particular <br> object, person, thing or event. |

Each has its own implications for learning and assessment.
To assess knowledge, skills and understanding we need to look for different things. Knowledge can be assessed to some extent through written tests, but the assessment of skills and deeper understanding requires different approaches. Because of this, the role of the teacher in assessment becomes much more important.

The assessment of $\mathrm{k}, \mathrm{u}, \mathrm{s}, \mathrm{v} / \mathrm{a}$ is elaborated in the graphics below;

## Knowledge

Knowledge is the easiest to assess because it is fairly straightforward to find out whether or not a learner has retained some information: a simple question can usually find this out. We ask them to name something, or state something, or label a diagram.

## Skills

Skills are the ability to perform a mental or physical operation, so we have to observe the skill being performed or look at the product, or outcome, of the skill; for example, a piece of writing, a picture or diagram.

Some skills, such as speaking or a physical education skill do not have a product so need to be observed.

## Understanding

Assessing deeper understanding is much more difficult, so we usually ask learners to explain, compare or outline a process. This can be done orally (in conversation) or in writing, and will give us some idea of the extent of their understanding.

## Values and Attitudes

Values and Attitudes determine how we interact with others, working in a team, meeting deadlines, being self-driven, holding democratic values, and having respect for democracy, race, gender, disability, human dignity, culture, nation, life and social justice. Some skills, such as speaking or a physical education skill do not have a product so need to be observed.

## Examinations

There will be examinations and tests set at the end of every level. Instead, there will be a summing up of on-going teacher assessments made in the context of learning.

## Formative Assessment

If assessment is to make a difference to teaching and learning, then teachers must use the information they gain from formative assessment to make some change to the teaching and learning process. If teaching and learning stay the same, there would have been no point in carrying out the assessment. The changes that can be made include decisions about:
i) What needs to be learned next
ii) Whether an element of the syllabus needs to be taught again in a different way
iii) Changing teaching approaches if necessary
iv) Identifying learners who need more support, or who are making exceptional progress
v) Enabling learners to understand what they have to do to improve

The final examination at the end of Cycle will be very different in nature, and will focus on the learners' ability to apply their learning in new situations, rather than on the ability to recall information.

It is the use of the assessment data within this cycle to improve learning that is key to the success and impact of formative assessment. It is this cycle that enables formative assessment to impact on learning:
i) The syllabus set out the learning outcomes
ii) The lessons seek to achieve these outcomes
iii) Assessment finds out whether or not the outcomes has been achieved
iv) This information guides the next steps in learning and so sets new learning outcomes

The process of teaching, making formative assessments and then changing the teaching and learning in some way can be seen as a cycle:


Formative assessment involves using all parts of the cycle
How to carryout formative assessments
In the AEP curriculum, the teacher's assessment role is not to write tests for learners, but to make professional judgements about learners' learning in the course of the normal teaching and learning process. The professional judgement is about how far the learner meets the Learning Outcomes that are set out in this syllabus. To make these judgements the teacher needs to look at how well the learners are performing in terms of each Learning Outcome.
School-based formative assessment is a part of the normal teaching and learning process, and so the assessment opportunities occur during this normal process. It is not something that needs to be added on after learning; it is an integral part of it.

These opportunities occur in three forms and are often called:
i) Observation - watching learners working (good for assessing skills and values)
ii) Conversation - asking questions, talking to learners, and learner to learner interactions (good for assessing knowledge and understanding)
iii) Product - appraising the learner's work (writing, report, translation, calculation, presentation, map, diagram, model, drawing, painting etc.). In this context, a "product" is seen as something physical and permanent that the teacher can keep and look at, not something that the learner says. When all three are used, the information from any one can be checked against the other two forms of assessment opportunity (e.g., evidence from "observation" can be checked against evidence from "conversation" and "product"). This is often referred to as "triangulation".

## Observation

## Product

Conversation

## Triangulation of assessment opportunities.

To find these opportunities, look at the syllabus units. These set out the learning that is expected and give 'Sample Assessment Activities", and in doing so they contain a range of opportunities for the three forms of assessment.

## Generic Skills

The Generic Skills have been built into the syllabus and are part of the Learning Outcomes. It is therefore not necessary to assess them separately. It is the increasingly complex context of the subject content that provides progression in the Generic Skills, and so they are assessed as part of the subject Learning Outcomes.

## Attitudes

It is not possible to assess attitudes in the same way as knowledge, understanding and skills because they are more personal and variable and are long-term aspirations. This does not mean that attitudes are not important. It means that we must value things that we cannot easily assess.

## Record Keeping

Keeping detailed records of learners' individual progress is always difficult with very large numbers of learners. For the purposes of school-based formative assessment, it is not even always necessary to keep such detailed records anyway. If feedback is given immediately and action is taken, then learning is changed and the record would soon become out of date and redundant.
Most formative class-based assessments are dynamic in that they feed straight back into the teaching and learning process. Therefore, detailed records of these are not appropriate.

What is needed is record of assessments of learners' learning made in terms of each Topic or unit. This means recording the on-going summative assessments of each topic. There is no need to make separate records of each of the Learning Outcomes because this would be very time-consuming and also unnecessary.
It is much more useful to make an overall assessment about whether or not each learner met the Learning Outcomes for each Topic as a whole.
Each Topic is made up of a number of Learning Outcomes. Therefore, teachers need to consider all the Learning Outcomes when making an overall judgement about the Topic as a whole. It is not always necessary for every individual Learning Outcome to be achieved for the Topic as a whole to be achieved. This will vary with the Subject and Topic.
By looking at the Learning Outcomes within each Topic, it is possible to identify four broad groups of learners in terms of their achievements:
There is no need to set a test to find this out.
These overall assessments should be made on the basis of the many formative assessments that the teacher has made during the course of teaching the Topic.

If teachers have been working with the learners over the course of the unit, they will be able to make a broad judgment about which learners have achieved or have failed to achieve the topic's overall Learning Expectation. These "Authentic Assessments" will be more valid and valuable than a test set by the school.

Recording these overall assessments will be simple, manageable and yet valuable, and can be recorded on a sheet such as the one below in which the categories are indicated with a number.

Although a very simple process, these four categories will give rich data when a comparison is made between the learners in each category for different subjects and units. They will also identify easily those learners who need extra support or who may not be ready to move on to the next grade at the end of a year.

If records are kept of the learning outcomes of each syllabus unit through the year, then there will be no need for an end of year test. Teachers will already have a record of those learners who have met the learning outcomes, and those who have not done so. Therefore, teachers will know if there were any learners not ready to progress to the next grade.
An overall record should be made of the individual topic assessments by subject in terms of the 3 descriptors. If numbers (1-3) are used as identifiers, then it will be possible to arrive at an overall number for a level by aggregating the identifiers for each topic.

| Descriptor | Identifier |
| :--- | :--- | :--- |
| Some LOs achieved, but not sufficient for overall <br> achievement. | 1 |
| Most LOs achieved, enough for overall achievement | 2 |
| All LOs achieved - achievement with ease. | 3 |

In the example below, the table shows the end-of-topic assessment for five learners.

|  | T1 | T2 | T3 | T4 | T5 | T6 | T7 | T8 | T9 | T10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Learner A | 3 | 3 | 2 | 3 | 3 | 3 | 3 | 2 | 3 | 3 |
| Learner B | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 | 3 | 2 |
| Learner C | 1 | 1 | 2 | 1 | 1 | 2 | 2 | 3 | 2 | 3 |
| Learner D | 1 | 1 | 2 | 1 | 1 | 2 | 1 | 1 | 2 | 1 |
| Learner E | 1 | 1 | 2 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

This method will give much more information than using a tick. For example, at a glance it can be seen that learners A \& B are achieving much higher than learners D \& E. It can be seen that Learner C has improved during the year. We can even see that more learners achieved success in Topic 9 than Topic 1.

All of this is very valuable assessment information and can be used to improve learning.

This summative teacher assessment will contribute $20 \%$ to the final grade of the School Leaving Certificate as elaborated in the Assessment Framework.

## Glossary of Key Terms

| TERM | DEFINITION |
| :--- | :--- |
| Competency | One in which learners develop the ability to apply <br> their learning with confidence in a range of situations. |
| Curriculum | The design or adaptation of learning experiences to <br> suit an individual learners' needs, strengths, <br> preferences, and abilities. |
| Formative | The process of judging a learner's performance, by <br> interpreting the responses to tasks, in order to gauge <br> progress and inform subsequent learning. |
| Assessment | Skills which are deployed in all subjects, and which <br> enhance the learning of those subjects. These skills <br> also equip young people for work and for life. |
| Inclusion | An approach to planning learning experiences which <br> allows each student to feel confident, respected and <br> safe and equipped to learn at his or her full potential. |
| Learning | A statement which specifies what the learner should <br> know, understand, or be able to do within a particular <br> aspect of a subject within a particular aspect of a <br> subject. |
| Outcome | A capability acquired by following the programme of <br> study in a particular subject; enables a learner to <br> apply the knowledge and understanding of the <br> subject. |
| Srocess Skill |  |




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